

Optimal Coupling to Obtain Higher Output Power in a Wireless Power Transmission System

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Abstract- In a WPT system, if its system parameters are designed unreasonably, output power and transmission efficiency will be low. Practical WPT must be able to support complicated coil configurations and keep following magnetic resonant conditions with maximum power transfer capability during coupling distance variation. The main parameters affecting output power and transmission efficiency are the distance between the coils, coupling coefficient, the resonance frequency and the resistance of the load. The maximum output power can be obtained in over coupled state by changing capacitor value of the resonating system. The proposed technique is analyzed with an equivalent circuit model, and simulations are performed to evaluate the performance. The system is validated through experimental results.

Index Terms- wireless power transmission, capacitance tuning, over coupled state.

1. INTRODUCTION

Two- and four-coil WPT systems have different topologies and are known by alternative names; for example, in the case of a two-coil WPT system, we have “inductive coupled WPT” or “inductively coupled power transfer” or “inductive WPT,” and in the case of a four-coil WPT system, we have “resonant coupled WPT” or “resonant WPT.” Additionally, the authors of [1] through [3] claimed that two-coil WPT systems are suitable for only short-range transmissions and that four-coil WPT systems are suitable for only mid-range transmissions. However, it was shown that there is no guarantee that both a two-coil WPT system and a four-coil WPT system will operate with identical primary and secondary coils, because the inductance either a two-coil, three-coil, or four-coil WPT system can be varied through an optimization process. As the coupling coefficient decreases, the real part of the

input impedance for a two-coil WPT system was shown to decrease, whereas that of a four-coil WPT system was shown to contrarily increase. These give rise to different suitable transmission distances for two-coil and four-coil WPT systems; however, their explanation is unfortunately oblique for readers to clearly understand the relation between the real part of the input impedance and the transmission distance. To describe how autonomous WPT system obey to the self-organization theory, we present an analysis based on a circuit model of a two-resonance system consisting of a transmitter resonator coupled to a receiver resonator.

Previously demonstrated magnetically coupled resonators used for WPT has shown the potential to deliver power with more efficiency than far-field approaches, and at longer ranges than traditional inductively coupled schemes. However, it appears frequency splitting phenomenon which is a physical phenomenon in mid-range WPT system. It occurs when the conditions for the maximum power theorem cannot be met at the resonance frequency of the resonators within the over-coupled region.

We know that Frequency splitting results decrease in output power. The main parameters affecting output power and transmission efficiency are the distance between the coils, coupling coefficient, resonance frequency and the resistance of the load. Here, we are online tuning method is applied by adjusting capacitance of the input matching network, and maximum output power is obtained in over coupled state.

2. MAXIMUM OUTPUT POWER OF CONVENTIONAL WPT SYSTEM

Applying kvl equations in fig. 1,

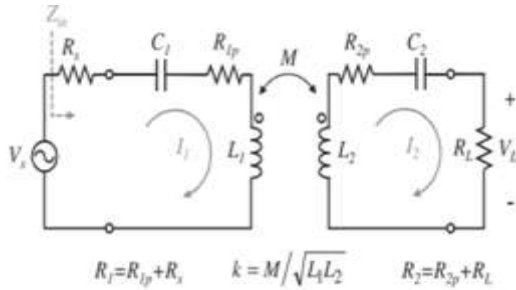


Fig. 1. Equivalent circuit model of a two-coil resonant WPT system.

$$V_s = (j\omega L_1 + 1/j\omega C_1 + R_1) \cdot I_1 - j\omega M \cdot I_2 \quad (1)$$

$$0 = -j\omega M \cdot I_1 + (j\omega L_2 + 1/j\omega C_2 + R_2) \cdot I_2 \quad (2)$$

The coupling coefficient k at critical coupling state become

$k_{critical} = 1/\sqrt{Q_1 Q_2}$ (3) where $Q_1 = \omega L_1 / (R_{1p} + R_s)$ $= \omega L_1 / R_1$ and $Q_2 = \omega L_2 / (R_{2p} + R_L) = \omega L_2 / R_2$ are the Q-factors of the primary coils and secondary coils. The free resonant angular frequencies are given by

$$\omega_1 = 1/\sqrt{L_1 C_1}, \quad \omega_2 = 1/\sqrt{L_2 C_2} \quad (4)$$

The output power and input power ratio is called energy efficiency of the system.

$$\eta = P_L / P_{in} = (R_L |I_2|^2 / |I_1|^2) / (R_1 + R_2 |I_2|^2 / |I_1|^2) \quad (5)$$

Where I_1 is the primary RMS current and I_2 is the secondary RMS current. From the equation (2),

$$|I_2 / I_1| = |(j\omega_0 k \sqrt{L_1 L_2}) / (j\omega_0 L_2 + 1/j\omega_0 C_2 + R_2)| \quad (6)$$

Here, $\omega_1 = \omega_2 = \omega_0$ substituting the equation (3) into equations (6) yields

$$|I_2 / I_1| = \sqrt{R_1 / R_2} \quad (7)$$

From (1) and (2),

$$|I_2 / V_s| = |j\omega M / ((j\omega_0 L_1 + 1/j\omega_0 C_1 + R_1)(j\omega_0 L_2 + 1/j\omega_0 C_2 + R_2) + \omega_0^2 M^2)| \quad (8)$$

Substitute equation (3) into (8),

$$|I_2 / V_s| = 1 / (2\sqrt{R_1 R_2}) \quad (9)$$

Critical coupling is the degree of coupling that provides maximum transfer of signal energy from one radio-frequency resonant circuit to another when both are tuned to the same frequency. Also known as optimum coupling. It can be represented only by using resistance parameters of resonating system.

The impedance input Z , in,

$$\begin{aligned} Z_{in} &= R_s + (R_{1p} + j\omega L_1 + 1/j\omega C_1) + [(\omega M)^2 / (R_2 + j\omega L_2 + 1/j\omega C_2)] \\ &= R_1 + Z_{reflected} \end{aligned} \quad (10)$$

Fig. 2 is the equivalent circuit diagram using the reflected impedance.

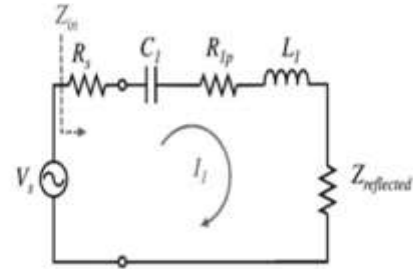


Fig. 2. Equivalent circuit model of Fig. 1 using reflected impedance.

$$Z_{reflected} = R_1 k^2 \cdot Q_1 Q_2 \quad (11)$$

Substituting (3) into (11), the reflected impedance $R_1 = (R_s + R_{1p})$, and the input impedance is $2R_1$. By doing this we get that the maximum power is transfers secondary resonator.

Substituting equation (7) to equation (5), we get the efficiency as

$$\eta = R_L / (2(R_{2p} + R_L)) \quad (12)$$

3. CRITICAL COUPLED STATE CONDITIONS FORMATION

If wireless power transfer system is over coupled at ω_0, ω_1 and ω_2 ,

$$|I_2 / I_1| = \sqrt{(k^2 L_1 / L_2) / ((\omega^2 / \omega_0^2 - 1)^2 + 1/Q_2^2)} \quad (13)$$

Comparing (7) with (13) gives

$$\omega_2 = \omega_0 \sqrt{(1 \pm \sqrt{(k^2 Q_2^2 - 1)(Q_1 - Q_2^2)})} \quad (14)$$

Similarly, the free resonant angular frequency of the primary resonator is also expressed as

$$\omega_1 = \omega_0 \sqrt{(1 \pm \sqrt{(k^2 Q_1^2 - 1)(Q_2 - Q_1^2)})} \quad (15)$$

If $Q_1 = Q_2$ and $Q_1, 2 \gg 1$, then equation (14) and (15) can be approximated as

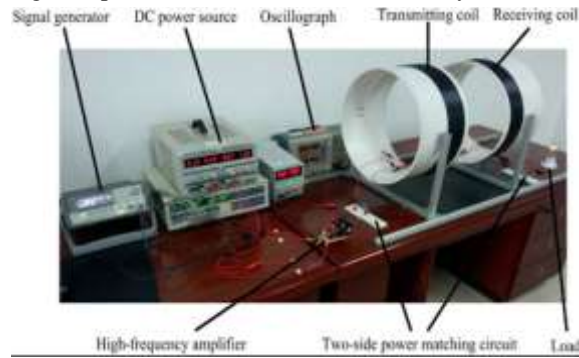
$$\omega_{1,2} \approx \omega_0 \sqrt{(1 \pm k)} \quad (16)$$

This is the frequency splitting by over coupling.

4. SIMULATION AND EXPERIMENTAL RESULTS

An experimental test rig whose measured circuit parameters are listed in Table 1 is set up in the laboratory. Both Tx and Rx sides have the same inductance and capacitance, so they share the same resonant frequency. For the resistance part there will be a flexibility for the change in parameter. All the resistance values such as r_1, r_2, R_{c1} , and R_{c2} are the practical measurement from the test rig.

Fig. 3 experimentation of two coil WPT system



Normally the distance between the two coils can be several times of the coil radius, which makes the coupling coefficient a very small value around 0.001 to 0.01.

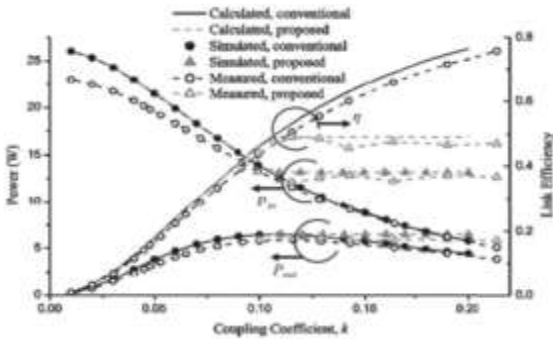


Fig. 4 Pout, Pin and efficiency with respect to k

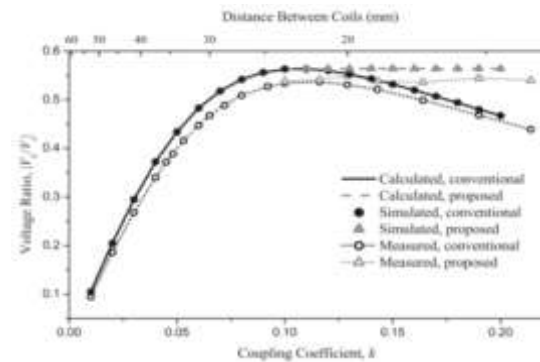


Fig.5 voltage gain with respect to k and coil distance

SYMBOL	NOTES	VALUE
Vs	input voltage ac rms	4.5 V
ω_0	Operating angular frequency	$2\pi \times 108 \times 10^3$ rad/s
L1	Primary inductance	24 μ H
L2	Secondary inductance	6.3 μ H
R1 p	Primary ESR	0.072 Ω
R2 p	Secondary ESR	0.019 Ω
Rs	Source resistance	0.7 Ω
RL	Load resistance	1.0 Ω

Table. 1 circuit parameters

Dis. [mm]	Coupling Coefficient	Free Resonant Freq. [kHz]	Desired Cap. [nF]	Adopted Caps. [nF]
14.0	0.214	112.4 128.5	83.6 243.4	82 1.5 220 22
15.5	0.190	111.7 125.6	84.5 254.8	82 2.2 220 33
17.0	0.164	111.0 122.2	85.7 269.3	82 3.9 150 120
18.5	0.143	110.3 119.0	86.8 283.8	82 4.7 180 100
20.0	0.129	109.8 116.5	87.6 296.2	82 4.7 180 120
21.5	0.116	109.1 113.5	88.7 312.2	82 6.8 220 100
23-61	0.1-0.01	108	90.5 344.7	68 22 220 120

Table. 2 series capacitance with respect to k

First we should measure coupling coefficient with respect to coil distance using E5061B analyser providing real time calculation. The offline tuning capacitance are detailed in Table.2. The calculated, experimental and simulated Pout, Pin, system efficiency and gain voltage with respect to k are shown in Fig. 4 and Fig. 5.

The proposed method is only applied in over coupled state and not in under coupled state. The simulation results and calculation results are appear to overlap, but results of experimentation are good with calculations. For the proposed system energy efficiency reaches to almost 50%. Free resonant frequencies are not equal to resonant frequencies.

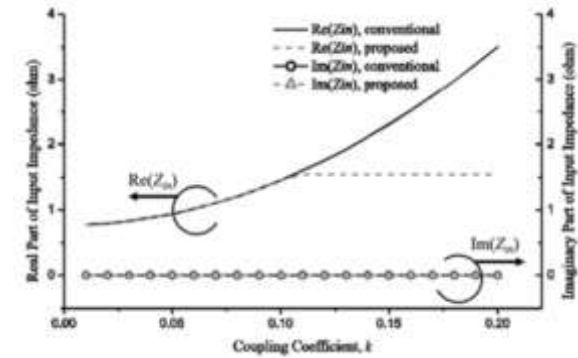


Fig. 6 simulated input impedance with respect to k

5. CONCLUSION

We implemented optimal coupling using frequency splitting to obtain higher power output, efficiency, gain and voltage. We know that splitting of frequencies results decrease in power output. The main parameters affecting output power and transmission efficiency are the distance between the

coils, coupling coefficient, resonance frequency and the resistance of the load.

Apart from the theoretical studies, the detailed implementation of wireless power transmission prototype including the design of coil, digital frequency generation, and large frequency power electronics is also introduced. Experiments are implemented to verify the effectiveness of circuit analysis by good tuning the circuit parameters. Because of large factors of the coils, the wireless power transmission is very sensitive to the jiggling and frequency drifting. From the circuit theory, the relationship between coupling coefficients power transfer, the circuit parameters and efficiency are analysed. The optimised work area balancing the distance and efficiency is introduced based on the analysis. In order to verify the WPT proposed circuit theories, a practical wireless power transmission prototype is formed and implemented in this paper.

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