

# Model Based Controller of pH Neutralization in Waste Water Treatment Process

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**Abstract-** Control of pH (hydrogen potential) neutralization process has always been one of the challenging problem in process control particularly in wastewater treatment. However, it is difficult to control a pH process with adequate performance point due to its nonlinearities, time-varying properties and sensitivity to small disturbances when working near the equivalence point. The pH level is controlled by adding NaOH or HNO<sub>3</sub> solution directly into the CSTR. A control mechanism must be applied in order to determine the amount of solution added to properly compensate for deviations in pH. By manipulating control parameters, the pH level within the system can be kept within a certain range. The PI and PID controllers are widely used in many industrial control systems because of its simple structure and robustness. MPC generates control actions by optimizing an objective function repeatedly over a finite moving prediction horizon, within system constraints, and MPC is implemented in simulation and compared with Ziegler and Nichols tuned PID.

**Index Terms-** Proportional Integral Derivative(PID),Model Predictive Control (MPC)

## I.INTRODUCTION

In recent years the industrial application of advanced control techniques for the process industries has become more demanding, mainly due to the increasing complexity of the processes themselves as well as to enhanced requirements in terms of product quality and environmental factors. Therefore the process industries require more reliable, accurate, robust, efficient and flexible control systems for the operation of process plant. In order to fulfill the above requirements there is a continuing need for research on improved forms of control. Control of industrial processes is a challenging task for several reasons due to their nonlinear dynamic behavior, uncertain and time varying parameters, constraints on manipulated variable, interaction between manipulated and

controlled variables, unmeasured and frequent disturbances, dead time on input and measurements.

Control of the pH process plays an important role in different chemical plants, such as chemical and biological reaction, waste water treatment, electrochemistry and precipitation plants, production of pharmaceuticals, fermentation, and food production such as in vegetable oil refining. However, it is difficult to control a pH process with adequate performance point due to its nonlinearities, time-varying properties and sensitivity to small disturbances when working near the equivalence point. More specifically, the pH was controlled in a continuously stirred tank reactor (CSTR) in this experiment. The reaction being controlled was the acid-base reaction of sodium hydroxide, NaOH, and Nitric acid, HNO<sub>3</sub>. The pH level is controlled by adding NaOH or HCl solution directly into the CSTR. A control mechanism must be applied in order to determine the amount of solution added to properly compensate for deviations in pH. By manipulating control parameters, the pH level within the system can be kept within a certain range.

Many of the control deals with design of linear controllers for linear systems. The proportional integral (PI) and proportional integral derivative (PID) controllers are widely used in many industrial control systems because of its simple structure and robustness. When it comes to the control of nonlinear and multivariable processes, the controller parameters have to be continuously adjusted. However, certain types of chemical systems or processes have highly nonlinear characteristics due to the reaction kinetics involved and the associated thermodynamic relationships. In these circumstances, conventional linear controllers no longer provide adequate and achievable control performance over the whole operating range. Thus, designing a nonlinear controller which is robust in terms of its

performance for different operating conditions is essential. There is also increasing interest in the potential of “intelligent” control methods for process applications.

Model Predictive Control also known as receding horizon control, is an advanced strategy for optimizing the performance of multivariable control systems. MPC generates control actions by optimizing an objective function repeatedly over a finite moving prediction horizon, within system constraints, and based on a model of the dynamic system to be controlled.

## II.HARDWARE DESCRIPTION

### A.EXPERIMENTAL SETUP

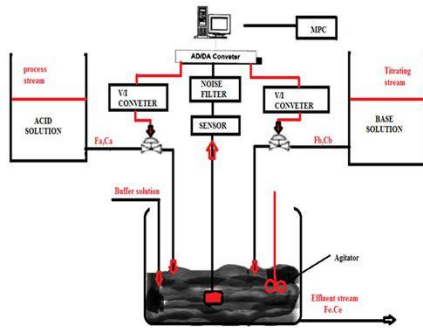


Fig.1 pH control system

Here pH of the process tank is the controlled variable, Inflow rate of the acid and base solution is the controlling variable. The controlled variable is the pH of the solution and the manipulated variable is the inflow of acid and base to the tank. The schematic diagram of the system is shown in the Fig.1

### B.BLOCK DIAGRAM

The pH value of the process tank should be maintained at a desired value. So, the controller is designed for the non-linear system and implemented using MATLAB software. The automatic process control block diagram is shown in the Fig. 2

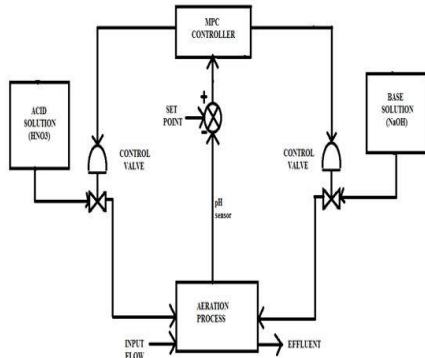


Fig.2Block diagram of pH control system

## III.MATHEMATICAL MODELING:

There are two streams of input and one stream of output.

**a:** acid stream with concentration  $C_a$  and flow rate  $F_a$

**b:** base stream with concentration  $C_b$  and flow rate  $F_b$

**bf:** buffer stream with concentration  $C(bf)$  and flow rate  $F(bf)$

**e:** effluent stream with concentration  $C_e$  and flow rate  $F_e$

Temperature maintains 25 degree Celsius

Density,  $\rho = \rho_a = \rho_b = \rho_{bf} = \rho_e$

Total mass balance:

Accumulation of total mass in the tank/time = [total input to the tank/time] – [total output from the tank/time]

$$\frac{d}{dt} \rho v = \rho_a F_a + \rho_b F_b + \rho(bf) F(bf) + \rho_e F_e$$

Based on assumption

$$\frac{d}{dt} v = f_a + f_b + f(bf) - f_e$$

Balance on component:

Accumulation of particular component in the tank/time = [total input of the component to the tank/time] – [total output from the tank]

$$\frac{d}{dt} (c_o, v) = [c_a \cdot f_a + c_b \cdot f_b + c(bf) \cdot f(bf)] - c_e \cdot f_e$$

According to the assumption that the stirrer in the CSTR well stirring takes place.

Hence say concentration of solution inside the tank and in the effluent stream will be same

$$\text{Hence } C_e = C_o$$

$$v \cdot \frac{d}{dt} (c_o) = (c_a - c_o) f_a + (c_b - c_o) f_b + (c(bf) - c_o) f(bf)$$

Taking Laplace transform of above equation

$$vs \cdot co(s) = (ca - co(s))fa(s) + (cb - co(s))fb(s) + (c(bf) - co(s))f(bf)(s)$$

$$\frac{co(s)}{fb(s)} = \frac{\{2 \cdot cb + \frac{c(bf) \cdot F(bf) \cdot ca}{fa \cdot cb}\}}{\{vs + fa \left[1 + \frac{ca}{cb}\right] + f(bf)\}}$$

TABLE 1 : Parameters of neutralization process

$(C_{HNO_3})_a$ = 0.003M	$(C_{HNO_3})_b$ = 0M	$(C_{HNO_3})_C = 0M$
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$(C_{NaHNO3})_a = 0M$	$(C_{NaHNO3})_b = 0.03M$	$(C_{NaHNO3})_c = 0.0005M$
$(C_{NaOH})_a = 0M$	$(C_{NaOH})_b = 0M$	$(C_{NaOH})_c = 0.003M$
$F_a = 16.6 mL/s$	$F_b = 0.55 mL/s$	$F_c = 15.5 mL/s$
$W_{1a} = 0.003M$	$W_{1b} = 0.0M$	$W_{1c} = 0.00035M$
$W_{2a} = 0M$	$W_{2a} = 0.03M$	$V = 2900ML$
$pK1 = 6.35$	$pK2 = 10.25$	$pH = 7.00$

Substituting these parameters in equation then the transfer function will be

$$\frac{C_{output}(s)}{f_{base}(s)} = Gp(s)$$

$$Gp(s) = \frac{3.14}{(15.4 s + 1)}$$

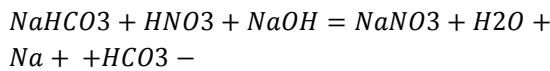
In this case concentration is taking as the output and flow rate of base is taking as input

**PARAMETER SELECTION**

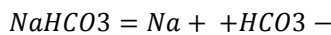
$NaHCO3$  = Sodium bicarbonate (buffer solution)

$HNO3$  = Nitric acid (acid solution)

$NaOH$  = sodium hydroxide (base solution)



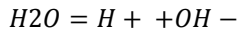
$NaHCO3$ 's aqueous solution is mainly alkaline due to the transformation of carbonic acid and hydroxide ion.



The pH number is a measure of concentration or more precisely the activity of hydrogen ion in a solution

$$pH = -Log[H+]$$

Water molecules are dissociated into hydrogen ion and hydroxyl ion according to the formula



In chemical equilibrium

$$\frac{[H +][OH -]}{H2O} = Constant$$

Only a small fraction of water molecules are split into ions. The water activity is practically unity and we get

$$[H +][OH -] = kw$$

Where kw is the equilibrium constant, has the value of  $10 - 14 \left[ \frac{mol}{l} \right]^2$  at  $25^\circ C$

Concentration of  $[NO3-]$  ion is considering  $Xa = Ca/v$

Concentration of  $[Na+]$  ion is considering  $Xb = Cb/v$

In this process, because of the acid and bases are completely ionized, Since the number of positive ions equal the number of negative ions. It follows that,  $Xa + [OH -] = Xb + [H+]$

The concentration of hydroxyl ion can be related to the hydrogen ion concentration. Hence

Solving for  $[H +]$  gives

$$[H +] = \frac{\left(\frac{X2}{4} + kw\right) 1}{2} - \frac{x}{2}$$

$$pH = -\log\left[\frac{\left(\frac{X2}{4} + kw\right) 1}{2} - \frac{x}{2}\right]$$

**IV.CONTROLLERS**

Controllers are basically employed in a closed loop control system. Closed loop control system is one that automatically changes the output based on the difference between the feedback signal to the input signal. Controller is an element used to produce manipulated variable from error variable, for control action.

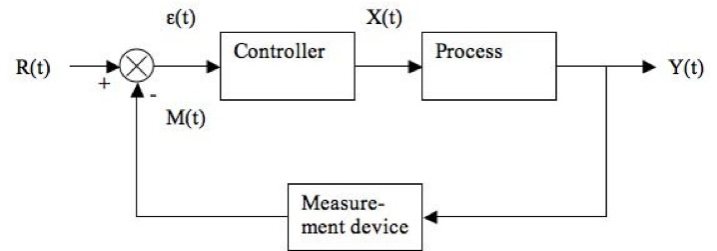


Fig.3 Controller in closed loop system

$R(t)$  – set point

$M(t)$  - feedback variable

$E(t)$  - error variable

$X(t)$  - manipulated variable

$Y(t)$  - controlled output variable

Basically, the electronic controllers are categorized into ON-OFF Control, Proportional(P) Controller, Proportional-Integral(PI) Controller,Proportional-Integral-Derivative(PID) Controller.

Among these controllers, PID is named as the best controller for its fast response, fast settling time and powerful control.

**A.PID CONTROLLER:**

A proportional–integral–derivative controller (PID controller) is a generic control loop feedback mechanism (controller) widely used in

industrial control systems – a PID is the most commonly used feedback controller. A PID controller calculates an "error" value as the difference between a measured process variable and a desired setpoint. The controller attempts to minimize the error by adjusting the process control inputs.

The PID controller calculation (algorithm) involves three separate constant parameters, and is accordingly sometimes called three-term control: the proportional, the integral and derivative values, denoted P, I, and D. Heuristically, these values can be interpreted in terms of time: P depends on the present error, I on the accumulation of past errors, and D is a prediction of future errors, based on current rate of change. The weighted sum of these three actions is used to adjust the process via a control element such as the position of a control valve, or the power supplied to a heating element.

**ZEIGLER NICHOLS OPEN LOOP TUNING**

The Zeigler Nichols Open-Loop Tuning Method is a way of relating the process parameters - delay time, process gain and time constant - to the controller parameters - controller gain and reset time. It has been developed for use on delay-followed-by-first-order-lag processes but can also be adapted to real processes.

Open loop response,  $K_p = 3.14$   
 Steady state value = 3.14  
 28.3% of the steady state value  $t_1 = 5.464$  sec  
 63.2% of the steady state value  $t_2 = 16.05$  sec  
 Time  $(T) = (t_2 - t_1)1.5 = (16.05 - 5.464)*1.5 = 7.057$  sec.  
 Time delay (td) =  $(t_2 - T) = (16.05 - 7.057) = 8.993$  sec

Transfer function of the given process,  

$$Gp(s) = \frac{3.14}{(15.4 s + 1)}$$

**CLOSED LOOP RESPONSE**

**PROPORTIONAL CONTROLLER**

$K_p = T / td \quad K_p = .25$

**PROPORTIONAL INTEGRAL CONTROLLER**

$K_c = (.9T) / td \quad K_p = .225$

$T_i = 3.33 td = 29.95$  sec

$K_i = K_c / T_i = .0075$  sec -1

**PROPORTIONAL INTEGRAL DERIVATIVE CONTROLLER**

$K_c = (1.2T) / td \quad K_p = .27$

$T_i = 2td = (2*8.993) = 17.986$  sec

$K_i = K_c / T_i = 0.015$  sec -1

$T_d = 0.5 td = 4.5$ sec

$K_d = K_c T_d = (.27*4.5) = 1.215$

**B.MODEL PREDICTIVE CONTROL**

Model predictive control (MPC), also known as receding horizon control or moving horizon control, uses the range of control methods, making the use of an explicit dynamic plant model to predict the effect of future reactions of the manipulated variables on the output and the control signal obtained by minimizing the cost function. The performance of the controller depends on how well the dynamics of the system being captured by the input-output model that is used for the design of the controller. Model predictive control is the family of controllers, makes the explicit use of model to obtain control signal. The reason for its popularity in industry and academia is its capability of operating without expert intervention for long periods.

Model Predictive Control, MPC, usually contains the following three ideas,

1. Explicit use of a model to predict the process output along a future time horizon.
2. Calculation of a control sequence to optimize a performance index.
3. A receding horizon strategy, so that at each instant the horizon is moved towards the Future, which involves the application of the first control signal of the sequence Calculated at each step.

The main advantage of MPC is the fact that it allows the current timeslot to be optimized, while keeping future timeslots in account. This is achieved by optimizing a finite time-horizon, but only implementing the current timeslot. MPC has the ability to anticipate future events and can take control actions accordingly.

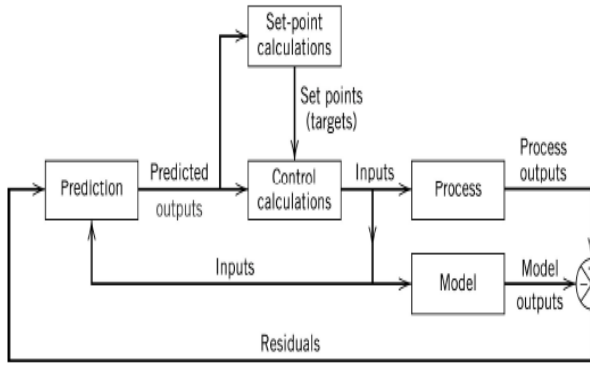


Fig.4 Block diagram of MPC

A block diagram of a model predictive control system is shown in Fig.6.3. A process model is used to predict the current values of the output variables. The residuals, the differences between the actual and predicted outputs, serve as the feedback signal to a Prediction block. The predictions are used in two types of MPC calculations that are performed at each sampling instant: set-point calculations and control calculations.

Inequality constraints on the input and output variables, such as upper and lower limits, can be included in either type of calculation. Note that the MPC configuration is similar to both the internal model control configuration and the Smith predictor configuration, because the model acts in parallel with the process and the residual serves as a feedback signal.

V.RESULTS AND DISCUSSIONS

Many real processes become unstable or out of specifications without controller. Because these reasons, a lot of processes can't be analyzed in open loop.

Now a frequency domain approach will be followed for the closed loop system. In each subsection a method will be discussed which can directly be implemented for the measurement of a closed loop system

PID Controller:

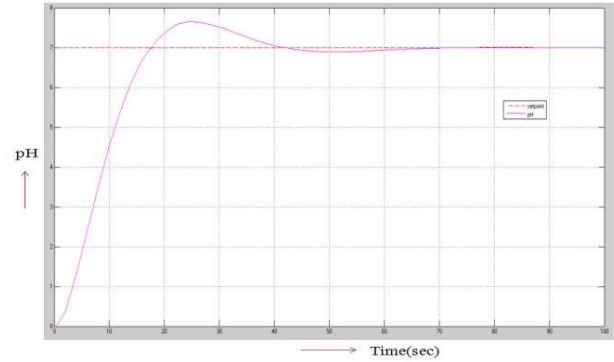


Fig.5 PID controller Model Predictive control (MPC)

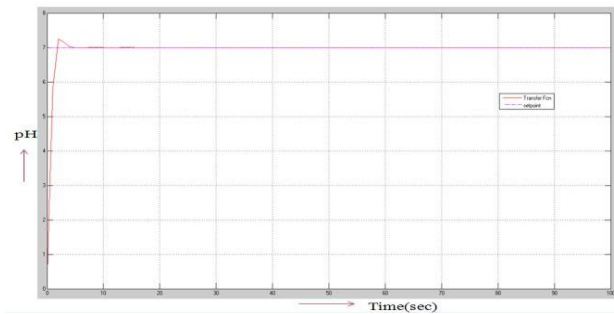


Fig.6 MPC response Comparison of P, PI, and PID controller

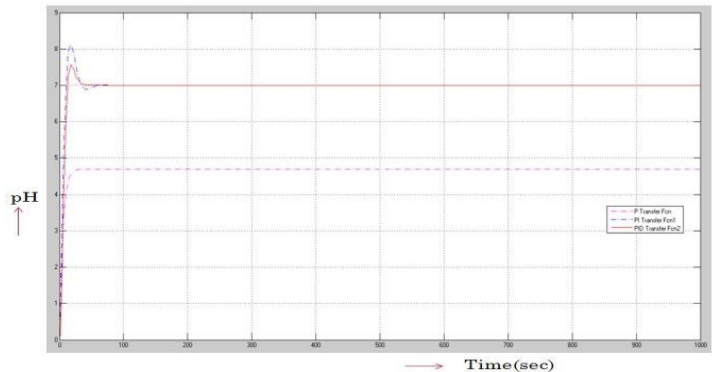


Fig .7 P, PI, PID comparison response

COMPARISON OF RESULTS IN SIMULATION

To Compare the Controller action various parameters such as settling time, Integral Absolute Error (IAE) and Integral Square Error (ISE) are taken.

Table 2 Comparison of results for PID and MPC

Parameters	PID controller	MPC
Settling Time(sec)	90	20

Integral Absolute Error (IAE)	69.21	4.851
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VI.CONCLUSION

pH control system is highly nonlinear parameter. In this project, the model of the pH control system is obtained using mathematical modeling and the transfer functions are obtained.. The conventional PID controller and MPC controller is designed and implemented in simulation. The predictive controller techniques provide better performance. The settling time, integral absolute error and integral square error was studied for the two controllers were studied. It is clear that MPC is faster when compared to PID.

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