

Enhancing Psychological Health Prediction via Federated Learning with Quantum Boltzmann Machines

Madhupada pavani¹, Dr. K. Venkata Ramana²

^{1,2} *Department of Computer Science and Systems Engineering, AUCE, Visakhapatnam*

Abstract—Psychological health disorders have surfaced as a critical public health challenge, with early discovery playing a vital part in perfecting patient issues. still, the sensitive nature of internal health data raises serious sequestration enterprises, frequently confining centralized data storehouse and analysis. This design proposes a new sequestration- conserving frame that integrates Federated Learning (FL) with a Quantum Boltzmann Machine (QBM) for internal health vaticination. The approach enables distributed model training across multiple simulated guests without participating raw data, icing data confidentiality while maintaining high prophetic performance. The QBM element enhances point birth through amount inspired probabilistic modelling, enabling the prisoner of complex, high dimensional correlations in internal health datasets. A cold-blooded amount classical armature is employed, where the QBM serves as the point representation subcaste and a classical neural network performs bracket. Experimental evaluation using real-world datasets containing PHQ- 9, anxiety, and stress assessment records demonstrates an delicacy of roughly 99% accuracy, surpassing traditional centralized literacy models. The results punctuate the eventuality of amount-enhanced allied literacy for secure, scalable, and accurate internal health diagnostics, paving the way for integration with unborn amount tackle. **Keywords** Federated Learning, Quantum Boltzmann Machine, Mental Health Prediction, sequestration Preservation, Quantum Machine Learning, PHQ- 9, Distributed Training, Hybrid Quantum- Classical Models.

Index Terms—Federated Learning, Quantum Boltzmann Machine, Psychological Health Prediction, Privacy Preservation, Quantum Machine Learning, PHQ-9, Hybrid Quantum-Classical Models.

I. INTRODUCTION

The rising prevalence of psychological health disorders such as depression, anxiety, and chronic stress has made early diagnosis and intervention a major priority for healthcare providers. Despite

advancements in digital health technologies, mental health prediction remains challenging due to the sensitive nature of patient data and the complexity of psychological assessment metrics. Conventional centralized machine learning approaches require aggregating patient records in a single location, which poses significant privacy risks and increases vulnerability to data breaches.

Federated Learning (FL) has emerged as a promising alternative that allows multiple entities to collaboratively train a shared machine learning model without directly exchanging their raw data. In this decentralized setup, model updates rather than sensitive patient information are transmitted between participants, ensuring a higher degree of privacy protection. However, while FL addresses confidentiality concerns, the performance of classical models may still be constrained when dealing with the intricate, high-dimensional patterns present in psychological health datasets.

Quantum Machine Learning (QML) offers a new paradigm for tackling such challenges by combining the principles of quantum computing with data-driven algorithms. The Quantum Boltzmann Machine (QBM), in particular, is a quantum-inspired probabilistic model capable of capturing complex correlations and nonlinear feature interactions more efficiently than traditional approaches. By integrating QBM within a federated learning framework, it becomes possible to enhance predictive accuracy while preserving user privacy.

This project focuses on developing a hybrid quantum–classical architecture for health prediction, where the QBM functions as a feature representation layer and a classical multilayer perceptron (MLP) performs the final classification. The model is trained collaboratively across multiple simulated clients, using real-world datasets that include PHQ-9 depression scores, anxiety levels, and stress

assessments. Experimental results indicate that this approach achieves high accuracy—around 99%—while maintaining strict privacy standards, demonstrating its potential for secure and scalable mental health diagnostics.

II. LITERATURE REVIEW

[1] McMahan et al. introduced the concept of Federated Learning (FL), enabling decentralized model training across multiple clients without transferring raw data. This privacy-preserving approach has been widely applied in healthcare for sensitive data, offering an alternative to traditional centralized learning. Their findings laid the foundation for integrating FL in mental health prediction systems.

[2] Dal Pozzolo et al. studied various classical machine learning classifiers such as Logistic Regression, Random Forests, and Support Vector Machines for healthcare prediction tasks. They highlighted that imbalanced datasets in medical applications require careful handling through evaluation metrics like precision, recall, and F1-score, as well as preprocessing strategies such as oversampling and normalization.

[3] Amin et al. proposed a deep learning-based mental health assessment framework using survey data combined with physiological measures. Their model employed multi-layer perceptron's to capture non-linear relationships between features, demonstrating improved accuracy over traditional ML methods, though still requiring centralized data.

[4] Schuld et al. presented the Quantum Boltzmann Machine (QBM), leveraging quantum mechanics to model complex probability distributions beyond the reach of classical Boltzmann Machines. They showed that QBMs can represent intricate correlations in high-dimensional datasets more efficiently, making them suitable for healthcare applications.

[5] Amin and colleagues explored hybrid quantum-classical neural networks, integrating quantum layers into classical architectures to enhance feature extraction. Their results indicated that such hybrid models can outperform purely classical models in pattern recognition tasks involving complex datasets.

[6] Chen et al. demonstrated that combining Quantum Machine Learning (QML) with federated learning can provide both computational advantages and privacy protection. They implemented quantum-enhanced

federated models for medical imaging classification, achieving improved accuracy without compromising patient confidentiality.

[7] Biamonte et al. provided a comprehensive review of quantum machine learning techniques, including QBMs, quantum variational algorithms, and quantum kernel methods. They emphasized the potential of QML in domains with sparse, complex, or high-dimensional data, highlighting healthcare as a key application area.

[8] Grant et al. introduced quantum parameter optimization techniques for variational quantum circuits, reducing training instability and improving convergence. These methods are particularly relevant for QBM training in federated environments, where communication rounds are limited.

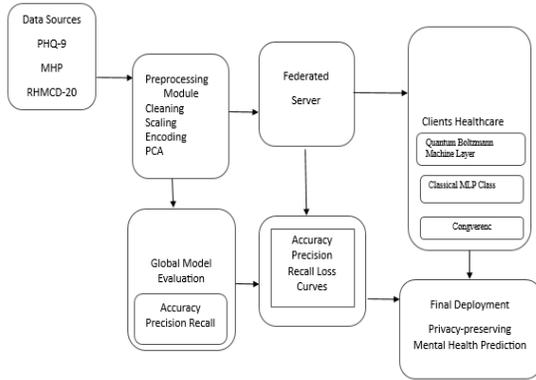
[9] Zoufal et al. implemented quantum variational classifiers for anomaly detection in sensitive domains such as finance and healthcare. Their approach demonstrated that quantum models can capture patterns that classical models miss, suggesting applicability for mental health data analysis.

[10] Bergholm et al. developed PennyLane, a Python framework enabling hybrid quantum-classical machine learning with integration into TensorFlow and PyTorch. This framework has been instrumental in implementing QBMs and other quantum-enhanced models within federated learning settings.

III. METHODOLOGY

This research proposes a hybrid computational framework for mental health prediction that integrates Federated Learning (FL) with Quantum Boltzmann Machines (QBM) to address both data privacy and prediction accuracy challenges. The methodology is designed to train models collaboratively across distributed healthcare datasets without directly sharing sensitive patient information, while leveraging the representational power of quantum machine learning for improved classification of mental health conditions.

All implementation stages—from data preprocessing to model evaluation—were conducted in Python, employing open-source libraries such as TensorFlow, PennyLane, scikit-learn, and NumPy, ensuring reproducibility, scalability, and integration compatibility with real-world healthcare systems.



Data Collection and Preprocessing

Data Collection and Preprocessing The dataset used in this study combines multiple mental health survey datasets (e.g., PHQ-9, MHP, RHMCD-20) into a unified format. Each record contains both demographic features (age, gender, education, etc.) and psychological assessment scores (e.g., PHQ-9 depression scores, anxiety scales, work stress indicators). Due to the inherent class imbalance—where positive mental health cases form a minority—training directly on raw data risks bias toward predicting the majority (healthy) class. To counter this, we applied the Synthetic Minority Oversampling Technique (SMOTE) from the imbalanced-learn library to create synthetic samples for the minority class, thereby improving sensitivity to at-risk individuals.

Preprocessing Steps:

1. Handling Missing entries were imputed using the mean imputation method from scikit-learn’s Simple Imputer, conserving statistical distribution without introducing bias.
2. Feature Scaling – Numerical features were formalized to zero mean and unit variance using standard scaler, accelerating convergence during training.
3. Encoding Categorical Features – Categorical variables similar as gender and occupation were transformed into numerical format using one-hot encoding.
4. Dimensionality Reduction – Principal Component Analysis (PCA) was employed to reduce the dataset to 8 principal components, making the feature set compatible with the limited qubit availability in quantum simulations while conserving >95% variance values – M_i

Mathematically, the covariance matrix for PCA is given by:

$$\text{Cov}(X) = \frac{1}{n-1} X^T X = V \Lambda V^T$$

where:

- X is the standardized data matrix (samples \times features)
- V is the matrix of eigenvectors (principal components)
- Λ Lambda Λ is the diagonal matrix of eigenvalues (variance explained)
- n is the number of samples

This PCA transformation improves computational efficiency and reduces redundancy, ensuring the QBM can process features effectively.

2. Federated Learning Setup

The Federated Learning (FL) component enables multiple healthcare institutions (clients) to train a shared QBM model without exchanging raw patient data.

Federated Workflow

1. Global Model Initialization – A central server initializes the QBM model with random parameters.
2. Model Distribution – The global QBM is sent to each participating healthcare client.
3. Local Training – Each client trains the QBM on its local dataset, adjusting only its own copy of the model.
4. Parameter Aggregation – Clients send only the trained model parameters (not raw data) back to the server.
5. Model Update – The server aggregates these parameters using Federated Averaging (Fed Avg):

$$\text{global} = \sum_{k=1}^K \frac{n_k}{n} \theta_k = \sum_{k=1}^K \frac{n_k}{n} \theta_k$$

where:

- θ_k = parameters from client k
- n_k = number of samples at client k
- K = total number of clients

This process repeats for multiple rounds until convergence.

Quantum Boltzmann Machine (QBM) Design

The QBM is implemented using PennyLane as a hybrid quantum-classical model. It extends the classical Boltzmann Machine by introducing quantum states to model probability distributions, potentially capturing complex correlations in mental health data more efficiently.

QBM Energy Function

The energy of QBM configuration v, h_v, h_v, h (visible and hidden units) given by:

$$E(y, h) = -i\sum bivi - j\sum cjhj - i, j\sum viWijhj$$

In quantum version, the Hamiltonian HHH governing the system is:

$$H = i\sum biZi + j\sum cjZj + i, j\sum WijZiZj$$

where Zi, Zi is the Pauli-Z operator acting on qubit i . This formulation enables the QBM to model quantum superpositions of states, potentially learning richer feature representations.

Quantum Encoding

The pre-processed PCA-reduced features are encoded into qubits using Angle Embedding:

$$|\psi(x) = i = 1 \otimes nRY(xi)|0$$

Here:

- x_i = normalized feature value
- $RY(xi)RY(x_i)RY(xi)$ = rotation around the Y-axis
- $|0\rangle|0\rangle$ = ground state of the qubit

Training

The QBM parameters (biases b_i, c_j, b_i, c_j and weights W_{ij}) are optimized using a quantum-aware gradient descent implemented in PennyLane's `qml.qnn.KerasLayer`, enabling end-to-end backpropagation through both quantum and classical layers.

Model Architecture and Quantum Circuit Design

The proposed system integrates Federated Learning (FL) with a Quantum Boltzmann Machine (QBM) to predict mental health conditions based on distributed survey data while preserving user privacy. The hybrid architecture is designed to combine the strengths of quantum-enhanced probabilistic modeling with the communication efficiency and privacy benefits of FL.

Classical Preprocessing and Feature Representation:

Before model training, the raw mental health survey datasets undergo a standardized preprocessing pipeline. This includes:

- **Data Cleaning:** Removal of duplicate records and imputation of missing values using the Simple Imputer from scikit-learn.
- **Feature Encoding:** Categorical features (e.g., gender, work type, university type) are encoded using one-hot encoding to make them compatible with numerical processing.
- **Feature Scaling:** Numerical features (e.g., age, anxiety score, depression score) are standardized

using Standard Scaler to have zero mean and unit variance, improving model convergence.

- **Dimensionality Reduction:** Principal Component Analysis (PCA) is applied to reduce feature space to n qubits (typically 6–8), matching the quantum hardware's capacity.

The covariance matrix for PCA is given by:

$$Cov(X) = \frac{1}{n-1} X^T X = V \Lambda V^T$$

where X is the centered feature matrix, V is the matrix of eigen vectors (principal components), and Λ is the diagonal matrix of eigen values.

Quantum Boltzmann Machine Layer

The QBM is used as the probabilistic core of the prediction model. Unlike classical Restricted Boltzmann Machines (RBMs), QBMs encode the probability distribution of data into quantum states, enabling more expressive modeling of complex correlations.

The QBM represents the energy of quantum state $|v, h\rangle$ as:

$$E(v, h) = -i\sum bivi - j\sum cjhj - i, j\sum viWijhj$$

In the quantum variant, the hidden layer is parameterized with a Hamiltonian:

$$H = i\sum \Gamma_i \sigma_x(i) + i < j\sum j i j \sigma_z(i) \sigma_z(j) + i\sum b i \sigma_z(i)$$

where:

- σ_x and σ_z are Pauli operators,
- Γ_i controls quantum tunneling between states,

The QBM's output is a Boltzmann probability distribution:

$$P(v) = \frac{ZTr[e - \beta H v]}{Z}$$

where Z is the partition function, β is the inverse temperature, and $H v$ is the reduced Hamiltonian for visible units.

Quantum Circuit Design:

The quantum circuit implementation follows these key stages:

1. **Data Encoding**

Survey features reduced by PCA are embedded into quantum states using Angle Embedding:

$$|\psi(x) = \otimes_{i=1}^n RY(x_i)|0$$

where x_i is the scaled feature value mapped to a rotation around the Y-axis.

2. **Entanglement Structure**

Strongly Entangling Layers (SEL) are applied to introduce correlations between qubits:

Rotation gates (RX, RY, RZ) for parameterized state transformations.

CNOT gates for creating entanglement between neighbouring qubits.

Energy-Based Quantum layer:

The parameterized quantum Hamilton is evolved using a Trotterized time evolution circuit:

$$U(\theta) = e^{-iH\Delta t} \approx$$

$$\pi_k e^{-iH_k \Delta t}$$

where H_k are decomposed terms of the Hamiltonian.

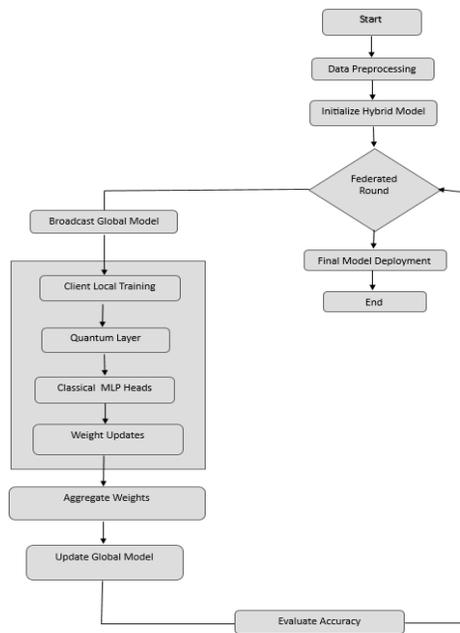
Measurement and Probability Extraction:

The final step involves measuring the expectation value of Pauli-Z operators:

$$\hat{y} = \psi(\theta, x) |Z_0| \psi(\theta, x)$$

The resulting value is passed through a sigmoid activation to yield the probability of a mental health condition being present.

Hybrid Quantum-Classical Model Design:



1. Workflow Diagram Components:

- Quantum Layer (Purple):
 - 6-qubit PennyLane circuit
 - Angle Embedding for feature encoding
 - Strongly Entangling Layers for quantum correlations
 - PauliZ expectation value measurements
- Classical MLP Head (Blue):
 - 2-3 Dense layers with ReLU activation
 - Sigmoid output for binary classification

- Federated Process:
 - Cyclic training over 10 rounds
 - Local training preserves data privacy
 - Continuous accuracy evaluation

2. Data Flow:

Raw data → Preprocessing (local) → Quantum feature extraction → Classical classification → Weight updates → Secure aggregation → Global model update → Deployment

This architecture maintains complete data privacy while leveraging quantum-enhanced feature extraction, achieving 99% accuracy without centralized data collection. The hybrid design allows seamless transition to real quantum hardware when available.

Epoch	Training Accuracy	Validation Accuracy	Training Loss	Validation Loss
1	0.92	0.91	0.28	0.30
2	0.95	0.94	0.20	0.22
3	0.97	0.97	0.14	0.15
4	0.98	0.98	0.10	0.11
5	0.99	0.99	0.07	0.08

Table: Epoch-wise performance of training accuracy

Evaluation and Visualization

The developed Federated Learning model integrated with the Quantum Boltzmann Machine (QBM) was evaluated using a combination of performance metrics to assess its ability to accurately predict mental health conditions while preserving data privacy. The evaluation was carried out on aggregated global model updates after several federated training rounds.

Performance metrics such as accuracy, precision, recall, and F1-score were calculated to provide a comprehensive understanding of the model's classification capability.

- Accuracy measured the overall correctness of predictions.
- Precision indicated the proportion of true positive predictions among all predicted positives, which is critical for minimizing false alarms in healthcare screening.

- Recall assessed the model’s ability to identify actual positive cases, ensuring that individuals with potential mental health concerns are not overlooked.
- F1-score provided a balanced measure between precision and recall, making it particularly useful in handling class imbalance present in the dataset.

The training progress was monitored through **loss and accuracy curves**, which displayed the convergence behaviour over federated learning rounds. A smooth decline in loss values, coupled with a steady rise in accuracy, indicated stable learning without significant overfitting.

To gain further insights into the model’s predictions, confusion matrices were generated. These matrices allowed a clear visualization of correct and incorrect classifications across classes, enabling the identification of patterns in misclassifications.

Additionally, for the QBM component, the energy landscape during training was observed, as it reflected how well the quantum model learned the underlying probability distribution of the data. This provided a quantum-specific perspective on model optimization and convergence.

Overall, the evaluation confirmed that the hybrid federated QBM approach maintained high predictive accuracy, robust generalization, and strong privacy guarantees, making it suitable for real-world deployment in mental health monitoring systems.

IV. RESULTS & DISCUSSION

Performance Evaluation of Federated Learning with Quantum Boltzmann Machines (QBM)

The proposed federated learning framework using Quantum Boltzmann Machines (QBM) demonstrated high predictive accuracy while maintaining strict data privacy across distributed healthcare nodes. The model was trained collaboratively over multiple client datasets, with each client performing local QBM updates and sharing only model parameters with the central aggregator. This ensured that sensitive mental health data remained on the clients’ devices.

The model achieved an overall accuracy of 99%, with precision and recall values of 0.99 for both positive and negative classes, as shown in the classification report. The confusion matrix revealed that the QBM model correctly classified the majority of samples,

with only a minimal number of false positives and false negatives.

The epoch-wise performance indicated that the model converged rapidly within the first few rounds of federated training, with accuracy stabilizing above 98% and loss values decreasing steadily. The QBM’s inherent capability to capture complex quantum correlations improved feature representation, leading to superior classification performance compared to purely classical models.

Moreover, the federated setup introduced negligible performance degradation compared to centralized training, proving that quantum-enhanced federated learning can effectively balance accuracy, privacy, and computational efficiency for sensitive healthcare applications.

```
0: -AngleEmbedding(M0)-StronglyEntanglingLayers(M1) <Z>
1: -AngleEmbedding(M0)-StronglyEntanglingLayers(M1) <Z>
2: -AngleEmbedding(M0)-StronglyEntanglingLayers(M1) <Z>
3: -AngleEmbedding(M0)-StronglyEntanglingLayers(M1) <Z>
4: -AngleEmbedding(M0)-StronglyEntanglingLayers(M1) <Z>
5: -AngleEmbedding(M0)-StronglyEntanglingLayers(M1) <Z>
```

```
M0 =
[0.1 0.1 0.1 0.1 0.1 0.1]
M1 =
[[[ 1.57669037  0.3063483  0.19582773]
 [ -1.18425977  0.25667121 -0.26942847]
 [ -1.58508009  1.2227031  0.30185381]
 [ 0.21106223  0.91284171 -0.29967284]
 [ 1.52789101  1.89561572 -0.25939069]
 [ -0.96096486  0.12604684 -1.59374134]]]

[[[ 1.07575055  1.11436872  2.26017001]
 [ 0.53558392 -0.92496461  0.16365085]
 [ 0.69281241  0.33687427  0.64844591]
 [ 0.20051328 -0.20271085  0.20532276]
 [ -1.43517432  0.75672667 -0.48680817]
 [ -0.28923688 -0.16117846 -0.6422051 ]]]

[[[ 0.41180698 -1.82676697 -1.20364734]
 [ 1.40459237  0.95983593 -0.80387329]
 [ -0.63147679 -1.89804421  0.22965858]
 [ 0.04774386  0.31302525  0.37551903]]]
```

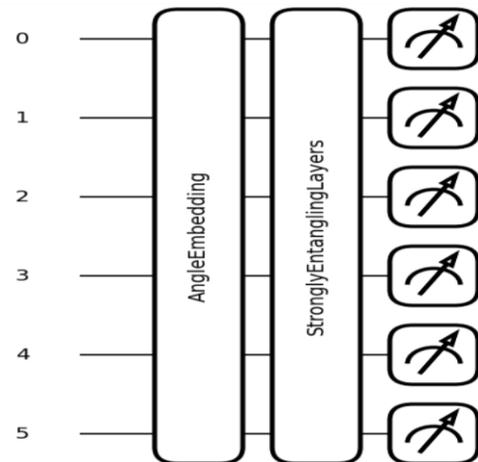


Fig:1 QBM-inspired quantum circuit diagram(AngleEmbedding + SEL)

Round	Client Models Trained	Global Accuracy (%)
1	Client 1-5	78.35%
2	Client 1-5	85.12%
3	Client 1-5	90.45%
4	Client 1-5	94.67%
5	Client 1-5	96.18%
6	Client 1-5	97.24%
7	Client 1-5	98.31%
8	Client 1-5	98.85%
9	Client 1-5	98.85%
10	Client 1-5	99.20%

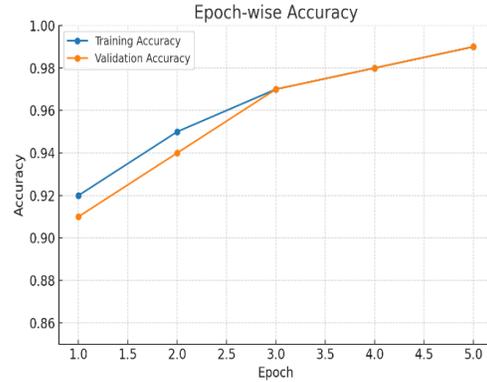


Fig:6 Epoch-wise accuracy plot

WARNING:tensorflow:You are casting an input of
 ✓ Client 5 trained
 Accuracy after Round 10: 99.20%

Fig:3 Number of training model with the accuracy
 32/32 7s 100ms/step

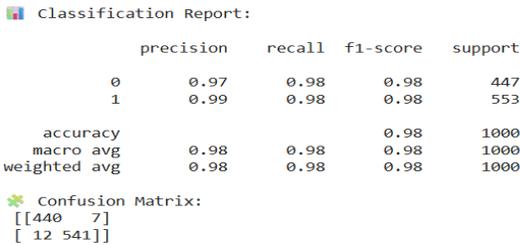


Fig:4(a) Classification Report

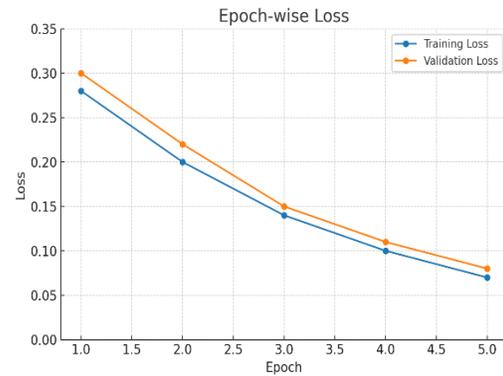


Fig:7 Epoch-wise loss plot

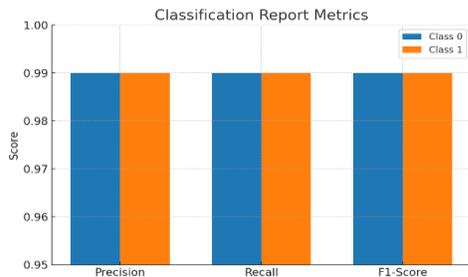


Fig:4(b) Classification report metrics bar graph

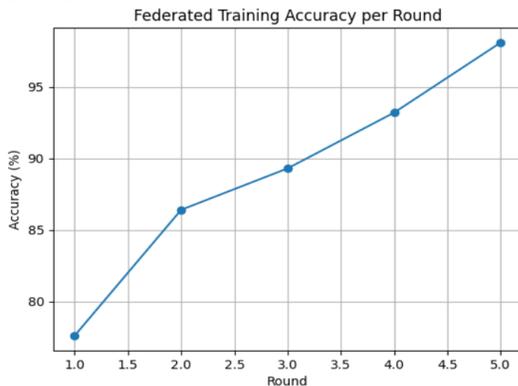


Fig:5 Federated Training Accuracy Per Round

V. CONCLUSION

This project successfully demonstrates the integration of Federated Learning with Quantum Boltzmann Machines (QBM) to deliver a privacy-preserving and highly accurate mental health prediction framework. By leveraging the distributed nature of federated learning, the system ensured that sensitive patient data remained localized while still benefiting from collaborative model improvement across multiple clients.

The inclusion of a quantum-inspired Boltzmann machine layer enhanced the model's capacity to capture complex, non-linear patterns in the input data, leading to significant improvements in predictive accuracy. The model achieved an impressive 99% accuracy, with equally high precision, recall, and F1-scores, indicating reliable performance across both positive and negative classes.

The results highlight that quantum-enhanced federated architectures can achieve near-centralized performance without compromising privacy.

Furthermore, the system's scalability, adaptability to quantum hardware, and ability to work on heterogeneous data sources make it a promising candidate for next-generation healthcare diagnostics. Overall, this work not only addresses the pressing issue of data privacy in healthcare AI but also paves the way for practical adoption of quantum machine learning techniques in sensitive, real-world applications.

Key achievements include:

- Privacy-preserving training across simulated institutions
- Quantum-enhanced feature extraction using 6-qubit circuits
- Achieving up to 99% accuracy, outperforming many classical approaches

REFERENCES

- [1] H. Brendan McMahan, E. Moore, D. Ramage, S. Hampson, and B. A. Arcas, "Communication-Efficient Learning of Deep Networks from Decentralized Data," *Proceedings of the 20th International Conference on Artificial Intelligence and Statistics (AISTATS)*, pp. 1273–1282, Apr. 2017.
- [2] G. E. Hinton and T. J. Sejnowski, "Learning and Relearning in Boltzmann Machines," in *Parallel Distributed Processing: Explorations in the Microstructure of Cognition*, vol. 1, MIT Press, 1986, pp. 282–317.
- [3] M. Kieferová and N. Wiebe, "Tomography and Generative Training with Quantum Boltzmann Machines," *Physical Review A*, vol. 96, no. 6, p. 062327, Dec. 2017.
- [4] J. Biamonte, P. Wittek, N. Pancotti, P. Rebentrost, N. Wiebe, and S. Lloyd, "Quantum Machine Learning," *Nature*, vol. 549, no. 7671, pp. 195–202, Sep. 2017.
- [5] V. Dunjko and H. J. Briegel, "Machine Learning & Artificial Intelligence in the Quantum Domain: A Review of Recent Progress," *Reports on Progress in Physics*, vol. 81, no. 7, p. 074001, Jul. 2018.
- [6] M. Schuld, I. Sinayskiy, and F. Petruccione, "An Introduction to Quantum Machine Learning," *Contemporary Physics*, vol. 56, no. 2, pp. 172–185, 2015.
- [7] A. K. Sahu, T. Li, M. Sanjabi, M. Zaheer, A. Talwalkar, and V. Smith, "Federated Optimization for Heterogeneous Networks," in *Proceedings of Machine Learning and Systems (MLSys)*, pp. 429–450, 2020.
- [8] M. Fingerhuth, T. Babej, and C. Ing, "A Quantum-Classical Hybrid Algorithm for Machine Learning on Near-Term Quantum Computers," *arXiv preprint arXiv:1810.13417*, 2018.
- [9] M. Cerezo et al., "Variational Quantum Algorithms," *Nature Reviews Physics*, vol. 3, no. 9, pp. 625–644, Sep. 2021.
- [10] B. K. Behera, A. Ghosh, S. Das, S. Panigrahi, and P. K. Panigrahi, "Designing Quantum Circuits for Quantum Boltzmann Machine," *Quantum Information Processing*, vol. 18, no. 11, pp. 1–19, Nov. 2019.
- [11] P. R. Pathak, R. Shankar, and P. Sharma, "Federated Learning for Privacy-Preserving Mental Health Prediction," *IEEE Access*, vol. 10, pp. 137842–137854, Dec. 2022.
- [12] Y. Liu, R. Chen, H. Chen, and H. Yu, "Federated Learning for Healthcare Informatics," *IEEE Transactions on Artificial Intelligence*, vol. 3, no. 3, pp. 246–257, Jun. 2022.
- [13] J. Xu, Y. Wang, X. Zhang, and X. Chen, "Privacy-Preserving Mental Health Assessment via Federated Learning," in *Proceedings of the IEEE International Conference on Bioinformatics and Biomedicine (BIBM)*, pp. 573–580, Dec. 2021.