

# Matrix Methods in Artificial Intelligence

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**Abstract**—Artificial Intelligence (AI) systems heavily rely on matrix methods derived from linear algebra. Matrices provide a structured and computationally efficient way to represent data, model relationships, and perform learning tasks. This paper explains matrix methods in AI with mathematical expressions and calculations.

## I. INTRODUCTION

Matrix operations form the backbone of AI algorithms such as machine learning, deep learning, computer vision, and natural language processing.

## II. MATRIX REPRESENTATION OF DATA

Let a dataset contain  $m$  samples and  $n$  features. It can be represented as a matrix:

$$X = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1n} \\ x_{21} & x_{22} & \dots & x_{2n} \\ \dots & \dots & \dots & \dots \\ x_{m1} & x_{m2} & \dots & x_{mn} \end{bmatrix}$$

## III. LINEAR REGRESSION USING MATRIX METHOD

The linear regression model is expressed as:

$$Y = XW$$

Where,

$X$  = input matrix

$W$  = weight matrix

$Y$  = output matrix

Calculation:

$$W = (X^T X)^{-1} X^T Y$$

Example:

$$X = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$Y = \begin{bmatrix} 5 \\ 6 \end{bmatrix}$$

## IV. MATRIX OPERATIONS IN NEURAL NETWORKS

Forward propagation is given by:

$$Z = XW + B$$

$$A = f(Z)$$

Backpropagation update rule:

$$W_{\text{new}} = W_{\text{old}} - \eta \frac{\partial L}{\partial W}$$

## V. EIGENVALUES IN AI

Eigenvalue equation:

$$AX = \lambda X$$

Used in PCA for dimensionality reduction.

## VI. SINGULAR VALUE DECOMPOSITION (SVD)

Any matrix  $A$  can be decomposed as:

$$A = U \Sigma V^T$$

Used in image compression and recommendation systems.

## VII. APPLICATIONS

1. Machine Learning
2. Deep Learning
3. Computer Vision
4. Natural Language Processing

## VIII. ADVANTAGES

1. Fast computation
2. Efficient storage
3. Scalability

## 9. CONCLUSION

Matrix methods are essential for building efficient and scalable AI systems.