

# An Extensive Review of Integral Transform

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**Abstract**— Integral transforms are among the most powerful and widely used mathematical tools in science and engineering. Many integral transformations have been proposed, tested, and successfully applied to solve problems arising in various scientific and technological fields. The importance of these transforms lies in their unique ability to convert complicated mathematical problems from one domain into another domain where simpler algebraic techniques can be employed. Because of this capability, integral transforms have become essential in solving differential equations, integral equations, boundary value problems, and systems of equations encountered in applied mathematics, physics, and engineering sciences.

In this study, we perform a quick survey of recent developments in Laplace type integral transforms.

**Index Terms**—Integral transform, Differential equation, Boundary value problem.

## I. INTRODUCTION

Integral transforms are important mathematical tools used to convert difficult differential equations into simpler algebraic equations. This method helps in solving complicated mathematical problems easily. In an integral transform, a function is multiplied by another function called the kernel and then integrated. The general form of an integral transform is

$$T\{f(t)\} = F(u) = \int_{t_1}^{t_2} f(t)K(t, u) dt$$

where  $f(t)$  is the input function,  $F(u)$  is the transformed function, and  $K(t, u)$  is the kernel of the transform.

In this paper we study the integral transform of Laplace type. Pierree-Simon Laplace pioneered the Laplace transform which is very useful and effective technique for solving initial and boundary value problems.

Over the years, many integral transforms have been proposed and most of these transforms have been named after the mathematicians who proposed them. Some integral transforms and their properties have been chronologically displayed in this work.

1.HY transform [46]:

The Hy transform of a continuous function  $f(t)$  is defined by

$$HY\{f(t)\} = u \int_0^\infty e^{-u^2 t} f(t) dt$$

HY transform of some elementary functions are

Function	HY transform
1	$\frac{1}{u}$
$t^n$	$\frac{n!}{u^{2n+1}}$
$e^{at}$	$\frac{u}{u^2 - a}$
$\sin at$	$\frac{au}{u^4 - a^2}$
$\cos at$	$\frac{u^3}{u^4 + a^2}$

HY transform of Derivatives

Let  $HY\{f(t)\} = F(u)$  then,

- i)  $HY\{f'(t)\} = u^2 F(u) - u f(0)$
- ii)  $HY\{f''(t)\} = u^4 F(u) - u^3 f(0) - u f'(0)$
- iii)  $HY\{f^n(t)\} = u^{2n} F(u) - \sum_{k=1}^{n-1} u^{2(n-k)-1} f^k(0)$

2.Bayawa Integral Transform [65]:

The Bayawa Integral Transform is defined as

$$B\{f(t)\} = \int_0^\infty K(s, t) f(t) dt$$

Where

- $K(s, t)$  is the kernel function,

- $f(t)$  is the original function
- $B\{f(t)\}$  denotes the transformed function.

$$M\{f(t)\} = \int_0^{\infty} e^{-st} f(t) dt$$

Properties of Bayawa Integral Transform

1) Linearity property:

If a and b are constants, then

$$B\{af(t) + bg(t)\} = aB\{f(t)\} + bB\{g(t)\}$$

Bayawa Integral of Derivatives:

- i)  $B\{f'(t)\} = sB\{f(t)\} - f(0)$
- ii)  $B\{f''(t)\} = s^2B\{f(t)\} - sf(0) - f'(0)$

3. Sharad Transform[10]

The Sharad Transform of a function  $f(t)$  is defined as

$$S\{f(t)\} = u \int_0^{\infty} e^{-st} f(t) dt$$

Where

- $f(t)$  is the original function.
- $s$  is the transform parameter.
- $S\{f(t)\}$  denotes the transformed function.

Sharad Transform of some elementary functions are

Function	Sharad Transform
1	$\frac{1}{s}$
t	$\frac{1}{s^2}$
$t^n$	$\frac{n!}{s^{n+1}}$
$e^{at}$	$\frac{1}{s-a}$
sinat	$\frac{a}{s^2 + a^2}$
cosat	$\frac{s}{s^2 + a^2}$

Properties of Sharad Transform

1) Linearity property

If a and b are constants, then

$$S\{af(t) + bg(t)\} = aS\{f(t)\} + bS\{g(t)\}$$

Sharad Transform of Derivatives

- i)  $S\{f'(t)\} = sS\{f(t)\} - f(0)$
- ii)  $S\{f''(t)\} = s^2S\{f(t)\} - sf(0) - f'(0)$

4. Mhase integral transform[66]:

Mhase integral transform of a function  $f(t)$  is defined as

Mhase integral transform of some elementary functions are

Function	Mhase integral transform
1	$\frac{1}{s}$
t	$\frac{1}{s^2}$
$t^n$	$\frac{n!}{s^{n+1}}$
$e^{at}$	$\frac{1}{s-a}$
sinat	$\frac{a}{s^2 + a^2}$
cosat	$\frac{s}{s^2 + a^2}$

Basic properties of Mhase integral transform

1) Linearity property

If a and b are constants, then

$$M\{af(t) + bg(t)\} = aM\{f(t)\} + bM\{g(t)\}$$

Mhase integral transform of Derivatives

- i)  $M\{f'(t)\} = sM\{F(t)\} - f(0)$
- ii)  $M\{f''(t)\} = s^2F(s) - sf(0) - f'(0)$

5. Khalouta Transform[32]:

The Khalouta Transform of a function  $f(t)$  is defined as

$$K\{f(t)\} = \int_0^{\infty} e^{-\frac{t}{s}} f(t) dt$$

Khalouta Transform of some elementary functions are

Function	Khalouta Transform
1	s
t	$s^2$
$t^n$	$n! s^{n+1}$
$e^{at}$	$\frac{s}{1-as}$
sinat	$\frac{as^2}{s^2 + a^2s^2}$
cosat	$\frac{s}{1 + a^2s^2}$

Basic properties of Khalouta Transform

1) Linearity property

If a and b are constants, then

$$K\{af(t) + bg(t)\} = aK\{f(t)\} + bK\{g(t)\}$$

2)Scaling property

$$K\{f(at)\} = \frac{1}{a} F\left(\frac{s}{a}\right)$$

Khalouta Transform of Derivatives

i)  $K\{f'(t)\} = \frac{1}{s}\{F(s)\} - f(0)$

ii)  $K\{f''(t)\} = \frac{1}{s^2}\{F(s)\} - \frac{f(0)}{s} - f'(0)$

6.Fareena Transform[67]:

Fareena Transform of a function f(t) is defined as

$$F\{f(t)\} = \int_0^\infty e^{-ut} f(t) dt$$

Fareena Transform of some elementary functions are

Function	Fareena Transform
1	1
t	$\frac{1}{u}$
$t^n$	$\frac{n!}{u^n}$
$e^{at}$	$\frac{1}{u-a}$
sinat	$\frac{au}{u^2 + a^2}$
cosat	$\frac{u^2}{u^2 + a^2}$

Basic properties of Fareena Transform

1)Linearity property:

If a and b are constants, then

$$F\{af(t) + bg(t)\} = aF\{f(t)\} + bF\{g(t)\}$$

Fareena Transform of Derivatives

i)  $K\{f'(t)\} = \frac{1}{s}\{F(s)\} - f(0)$

ii)  $K\{f''(t)\} = \frac{1}{s^2}\{F(s)\} - \frac{f(0)}{s} - f'(0)$

7.Ramadhan Group Transform[47]

Ramadhan Group Transform of a function f(t) is defined as

$$R\{f(t)\} = \frac{1}{u} \int_0^\infty e^{-st} f(t) dt$$

Ramadhan Group Transform of some elementary functions are

Function	Ramadhan Group Transform
1	$\frac{1}{us}$
t	$\frac{1}{us^2}$

$t^n$	$\frac{n!}{us^{n+1}}$
$e^{at}$	$\frac{1}{u(s-a)}$
sinat	$\frac{a}{u(s^2 + a^2)}$

Basic properties of Ramdhan Group Transform

1)Linearity property

If a and b are constants, then

$$R\{af(t) + bg(t)\} = aR\{f(t)\} + bR\{g(t)\}$$

II)Scaling property

$$R\{f(at)\} = \frac{1}{a} F\left(\frac{s}{a}\right)$$

Ramadhan Group Transform of Derivatives

i)  $R\{f'(t)\} = s\{F(s)\} - \frac{f(0)}{u}$

ii)  $R\{f''(t)\} = s^2\{F(s)\} - \frac{sf(0)}{s} - f'(0)$

8.Kashuri and Fundo Transform[68]

The Kashuri and Fundo Transform of a function f(t) is defined as

$$KF\{f(t)\} = u \int_0^\infty e^{-ut} f(t) dt$$

Where

u is the transform parameter,

f(t) is the original function

KF{f(t)} denotes the transformed function.

Kashuri and Fundo Transform of some elementary functions are

Function	Kashuri and Fundo Transform
1	1
t	$\frac{1}{u}$
$t^n$	$\frac{n!}{u^n}$
$e^{at}$	$\frac{1}{u-a}$
sinat	$\frac{au}{u^2 + a^2}$
cosat	$\frac{u^2}{u^2 + a^2}$
sinhat	$\frac{au}{u^2 - a^2}$
coshat	$\frac{u^2}{u^2 - a^2}$

Basic properties Kashuri and Fundo Transform

1)Linearity property

If a and b are constants ,then

$$KF\{af(t) + bg(t)\} = aKF\{f(t)\} + bKF\{g(t)\}$$

II)Scaling property

$$KF\{e^{at}f(t)\} = F(u - a)$$

Kashuri and Fundo Transform of Derivatives:

i)  $KF\{f'(t)\} = uKF\{F(t)\} - uf(0)$

ii)  $KF\{f''(t)\} = u^2KF\{F(t)\} - u^2f(0) - uf'(0)$

9.Kamal transform[27]

The Kamal transform of a function f(t)is defined by

$$K\{f(t)\} = \int_0^\infty e^{-\frac{t}{u}} f(t)dt$$

where uis the transform parameter.

Kamal transformof some elementary functions are

Function	Kamal transform
1	u
t	u <sup>2</sup>
t <sup>n</sup>	n! u <sup>n+1</sup>
e <sup>at</sup>	$\frac{u}{1 - au}$
sinat	$\frac{au^2}{1 + a^2u^2}$
cosat	$\frac{u}{1 + a^2u^2}$

Properties Kamal transform

1)Linearity property

If a and b are constant, then

$$K\{af(t) + bg(t)\} = aK\{f(t)\} + bK\{g(t)\}$$

2)Scaling property

$$K\{f(at)\} = \frac{1}{a} F\left(\frac{s}{a}\right)$$

Kamal transform of Derivatives

i)  $K\{f'(t)\} = \frac{1}{u}\{F(u)\} - f(0)$

ii)  $K\{f''(t)\} = \frac{1}{u^2} F(u) - \frac{f(0)}{u} - f'(0)$

10.Mahgoub Transform[36]

The Mahgoub Transform of a function f(t)is defined by

$$M\{f(t)\} = s \int_0^\infty e^{-st} f(t)dt$$

Function	Mahgoub Transform
1	1

t	$\frac{1}{s}$
t <sup>n</sup>	$\frac{n!}{s^{n+1}}$
e <sup>at</sup>	$\frac{s}{s - a}$
sinat	$\frac{as}{s^2 + a^2}$
cosat	$\frac{s^2}{s^2 + a^2}$

Properties of Mahgoub Transform

1)Linearity property

If a and b are constants ,then

$$M\{af(t) + bg(t)\} = aM\{f(t)\} + bM\{g(t)\}$$

2)Exponential Shift property

$$M\{e^{at}f(t)\} = F(u - a)$$

Mahgoub Transform of Derivatives

i)  $M\{f'(t)\} = uM\{f(t)\} - u^2f(0)$

ii)  $M\{f''(t)\} = u^2M\{f(t)\} - u^3f(0) - u^2f'(0)$

11.Tarig Transform[16]

The Tarig Transform of a function f(t)is defined by

$$T\{f(t)\} = \frac{1}{u} \int_0^\infty e^{-ut} f(t)dt$$

Function	Tarig Transform
1	$\frac{1}{u^2}$
t	$\frac{1}{u^3}$
t <sup>n</sup>	$\frac{n!}{u^{n+2}}$
e <sup>at</sup>	$\frac{1}{u(u - a)}$

Properties of Tarig Transform

1)Linearity property

If a and b are constants, then

$$T\{af(t) + bg(t)\} = aT\{f(t)\} + bT\{g(t)\}$$

2)Scaling property

$$T\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

Tarig Transform of Derivatives

i)  $T\{f'(t)\} = uT\{f(t)\} - \frac{f(0)}{u}$

12.Sadik Transform[34]

The Sadik Transform of a function f(t)is defined by

$$S\{f(t)\} = \frac{1}{v^\infty} \int_0^\infty e^{-\frac{st}{v}} f(t)dt$$

Function	Sadik Transform
1	$\frac{v^{1-\alpha}}{s}$
t	$\frac{v^{2-\alpha}}{s^2}$
t <sup>n</sup>	$\frac{n! v^{n+1-\alpha}}{s^{n+1}}$

Properties of Sadik Transform

1)Linearity property

If a and b are constants, then

$$S\{af(t) + bg(t)\} = aS\{f(t)\} + bS\{g(t)\}$$

2)Exponential Shift property

$$S\{e^{at}f(t)\} = F(s - av)$$

Sadik Transform of Derivatives

$$T\{f'(t)\} = \frac{s}{v} S\{F(s)\} - \frac{f(0)}{v^\alpha}$$

13.Yang Transform[69]

The Yang Transform of a function f(t)is defined by

$$Y\{f(t)\} = \int_0^\infty e^{-\frac{t}{u}} f(t)dt$$

Yang Transform of some elementary functions are

Function	Yang Transform
1	u
t	u <sup>2</sup>
e <sup>at</sup>	$\frac{u}{1 - au}$

Properties of Yang Transform

1)Linearity property

If a and b are constants, then

$$Y\{af(t) + bg(t)\} = aY\{f(t)\} + bY\{g(t)\}$$

Yang Transform of Derivatives

$$Y\{f'(t)\} = \frac{1}{u} T(u) - f(0)$$

14.Shehu Transform[42]

The Shehu Transform of a function f(t)is defined by

$$S\{f(t)\} = \int_0^\infty e^{-\frac{st}{u}} f(t)dt$$

Shehu Transform of some elementary functions are

Function	Shehu Transform
1	$\frac{u}{s}$
t	$\frac{u^2}{s^2}$

e <sup>at</sup>	$\frac{u}{s - au}$
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Properties of Shehu Transform

1)Linearity property

If a and b are constants, then

$$S\{af(t) + bg(t)\} = aS\{f(t)\} + bS\{g(t)\}$$

2)Scaling property

$$S\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

Shehu Transform of Derivatives:

$$S\{f'(t)\} = \frac{s}{u} F(u, s) - f(0)$$

15.Sawi Transform [38]

The Sawi Transform of a function f(t)is defined by

$$S\{f(t)\} = \frac{1}{u^2} \int_0^\infty e^{-\frac{t}{u}} f(t)dt$$

Sawi Transform of some elementary functions are

Function	Sawi Transform
1	$\frac{1}{u}$
t	1

1)Linearity property

If a and b are constants ,then

$$S\{af(t) + bg(t)\} = aS\{f(t)\} + bS\{g(t)\}$$

Sawi Transform of Derivatives

$$S\{f'(t)\} = \frac{1}{u} F(u) - \frac{f(0)}{u^2}$$

16.Barne’s Polynomial Integral Transform[70]

The Barne’s Polynomial Integral Transform of a function f(t)is defined by

$$B\{f(t)\} = \frac{1}{u} \int_0^\infty P_n(t)e^{-st} f(t)dt$$

1)Linearity property:

If a and b are constants ,then

$$B\{af(t) + bg(t)\} = aB\{f(t)\} + bB\{g(t)\}$$

Barne’s Polynomial Integral Transform of Derivatives

i)  $B\{f'(t)\} = sF(s) - f(0)$

17. Atangana Kilicman Integral Transform[8]

Atangana Kilicman Integral Transform of a function  $f(t)$  is defined by

$$A\{f(t)\} = s^n \int_0^\infty e^{-st} f(t) dt$$

Function	Atangana Kilicman Integral Transform
1	$s^{n-1}$
$t^m$	$n! u^{n+1}$

Properties of Atangana Kilicman Integral Transform

1) Linearity property

If a and b are constants, then

$$A\{af(t) + bg(t)\} = aA\{f(t)\} + bA\{g(t)\}$$

Atangana Kilicman Integral Transform of Derivatives

i)  $A\{f'(t)\} = sA\{f(t)\} - s^n f(0)$

18. Hankel Transform[71]

Hankel Transform of a function  $f(t)$  is defined by

$$H_n\{f(t)\} = s^n \int_0^\infty rf(r) J_n(sr) dr$$

where  $J_n(sr)$  is the Bessel function of first kind.

Properties of Properties of Atangana Kilicman Integral Transform

1) Linearity property

If a and b are constants, then

$$H_n\{af(r) + bg(r)\} = aH_n\{f(r)\} + bH_n\{g(r)\}$$

Hankel Transform of Derivatives

i)  $H_n\left\{\frac{df}{dr}\right\} = -sH_{n+1} f(r)$

19. Kharrat Toma Transform[41]

Kharrat Toma Transform of a function  $f(t)$  is defined by

$$KT\{f(t)\} = s^2 \int_0^\infty e^{-st} f(t) dt$$

Kharrat Toma Transform of some elementary functions are

Function	Kharrat Toma Transform

1	s
t	1
$t^n$	$\frac{n!}{s^{n-1}}$

Properties of Properties of Kharrat Toma Integral Transform

1) Linearity property

If a and b are constants, then

$$KT\{af(t) + bg(t)\} = aKT\{f(t)\} + bKT\{g(t)\}$$

Kharrat Toma of Derivatives

$$KT\{f'(t)\} = sKT\{f(t)\} - s^2 f(0)$$

20. Alenzi Transform[72]

The Alenzi transform of a function  $f(t)$  is defined as

$$A\{f(t)\} = u \int_0^\infty e^{-\frac{t}{u}} f(t) dt$$

Alenzi Transform of some elementary functions are

Function	Alenzi Transform
t	$u^2$
$t^2$	$u^3$
$t^n$	$n! u^{n+2}$
$e^{at}$	$\frac{u^2}{1-au}$
$\sin at$	$\frac{au^3}{1+a^2u^2}$
$\cos at$	$\frac{u^2}{1+a^2u^2}$

Properties of Properties of Alenzi Transform

1) Linearity property

If a and b are constants, then

$$A\{af(t) + bg(t)\} = aA\{f(t)\} + bA\{g(t)\}$$

II) Scaling property

$$A\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

III) Exponential Shift property

$$A\{e^{at}f(t)\} = F\left(\frac{u}{1-au}\right)$$

Alenzi Transform of Derivatives

$$A\{f'(t)\} = \frac{1}{u}\{F(u)\} - uf(0)$$

ii)  $A\{f''(t)\} = \frac{1}{u^2}F(u) - \frac{f(0)}{u} - uf'(0)$

21.W Transform[56]

The W transform is defined by

$$W\{f(t)\} = \frac{1}{u} \int_0^{\infty} e^{-\frac{t}{u}} f(t) dt$$

W Transform of some elementary functions are

Function	W Transform
1	1
t	u
t <sup>n</sup>	n! u <sup>n</sup>
e <sup>at</sup>	$\frac{1}{1-au}$
sinat	$\frac{au}{1+a^2u^2}$
cosat	$\frac{1}{1+a^2s^2}$

Properties of Properties W Transform

1)Linearity property

If a and b are constants, then

$$W\{af(t) + bg(t)\} = aW\{f(t)\} + bW\{g(t)\}$$

2)Scaling property

$$W\{f(at)\} = \frac{1}{a}F\left(\frac{u}{a}\right)$$

W Transform of Derivatives:

i)  $W\{f'(t)\} = \frac{1}{u}\{F(u)\} - \frac{1}{u}f(0)$

ii)  $W\{f''(t)\} = \frac{1}{u^2}F(u) - \frac{f(0)}{u^2} - uf'(0)$

22.Pourreza Transform[73]

The Pourreza transform is defined as

$$P\{f(t)\} = s \int_0^{\infty} f(t) e^{-st} dt$$

Pourreza Transform of some elementary functions are

Function	Pourreza Transform

1	1
t	$\frac{1}{s}$
t <sup>n</sup>	$\frac{n!}{s^n}$
e <sup>at</sup>	$\frac{s}{s-a}$
sin at	$\frac{as}{s^2+a^2}$
cos at	$\frac{s^2}{s^2+a^2}$

Properties of Properties Pourreza transform

i) Linearity Property

$$P\{af(t) + bg(t)\} = aP\{f(t)\} + bP\{g(t)\}$$

ii) Exponential Shift Property

$$P\{e^{at}f(t)\} = F(s-a)$$

Pourreza transform of Derivatives

i)  $P\{f'(t)\} = sP\{f(t)\} - sf(0)$

ii)  $P\{f''(t)\} = s^2P\{f(t)\} - s^2f(0) - sf'(0)$

23.G-Transform[13]

The G-transform of a function f(t) is defined by

$$G\{f(t)\} = \int_0^{\infty} f(t) e^{-st/u} dt$$

G-transform of some elementary functions are

Function	G-transform
1	$\frac{u}{s}$
t	$\frac{u^2}{s^2}$
t <sup>n</sup>	$\frac{n! u^{n+1}}{s^{n+1}}$
e <sup>at</sup>	$\frac{u}{s-au}$

Properties of Pourreza transform

i) Linearity Property

$$G\{af(t) + bg(t)\} = aG\{f(t)\} + bG\{g(t)\}$$

(ii) Scaling Property

$$G\{f(at)\} = \frac{1}{a}F\left(\frac{s}{au}\right)$$

G-transform of Derivatives

i)  $G\{f'(t)\} = \frac{s}{u}F(s,u) - f(0)$

ii)  $G\{f''(t)\} = \frac{s^2}{u^2}F(s,u) - \frac{s}{u}f(0) - f'(0)$

24. Formable Transform[73]

The Formable transform is defined as

$$F\{f(t)\} = u \int_0^{\infty} f(t) e^{-st/u} dt$$

Formable transform of some elementary functions are

Function	G-transform
1	$\frac{u^2}{s}$
t	$\frac{u^3}{s^2}$
t <sup>n</sup>	$\frac{n! u^{n+2}}{s^{n+1}}$
e <sup>at</sup>	$\frac{u^2}{s - au}$

Properties of Formable transform

i) Linearity Property

$$F\{af(t) + bg(t)\} = aF\{f(t)\} + bF\{g(t)\}$$

(ii) Exponential Shift Property

$$F\{e^{at}f(t)\} = F(s - au)$$

Formable transform of Derivatives

i)  $F\{f'(t)\} = \frac{s}{u} F(s, u) - uf(0)$

ii)  $F\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - sf(0) - uf'(0)$

25. ARA Transform[49]

The ARA transform of a function f(t) is defined by

$$A\{f(t)\} = s^n \int_0^{\infty} f(t) e^{-st} dt$$

ARA transform of some elementary functions are

Function	ARA transform
1	$s^{n-1}$
t	$s^{n-2}$
t <sup>m</sup>	$\frac{m!}{s^{m-n+1}}$
e <sup>at</sup>	$\frac{s^n}{s - a}$

Properties of ARA transform

1) Linearity Property

$$A\{af(t) + bg(t)\} = aA\{f(t)\} + bA\{g(t)\}$$

2) Scaling Property

$$A\{f(at)\} = \frac{1}{a^n} F\left(\frac{s}{a}\right)$$

ARA transform of Derivatives

i)  $A\{f'(t)\} = sA\{f(t)\} - s^n f(0)$

ii)  $A\{f''(t)\} = s^2 A\{f(t)\} - s^{n+1} f(0) - s^n f'(0)$

26. Kushare Transform[33]

The Kushare transform of a function f(t) is defined by

$$K\{f(t)\} = s \int_0^{\infty} f(t) e^{-t} dt$$

Kushare transform of some elementary functions are

Function	Kushare transform
1	s
t <sup>n</sup>	n! s
e <sup>at</sup>	$\frac{s}{1 - a}$
sin at	$\frac{as}{1 + a^2}$
cos at	$\frac{s}{1 + a^2}$

Properties of Kushare transform

1) Linearity Property

$$K\{af(t) + bg(t)\} = aK\{f(t)\} + bK\{g(t)\}$$

2) Shifting Property

$$K\{e^{at}f(t)\} = F(s - a)$$

Kushare transform of Derivatives

i)  $K\{f'(t)\} = F(s) - sf(0)$

ii)  $K\{f''(t)\} = F(s) - sf(0) - sf'(0)$

27. Soham Transform[45]

The Soham transform is defined as

$$S\{f(t)\} = \int_0^{\infty} f(t) e^{-t/u} dt$$

Soham transform of some elementary functions are

Function	Soham transform
1	u
t	u <sup>2</sup>
t <sup>n</sup>	n! u <sup>n+1</sup>
e <sup>at</sup>	$\frac{u}{1 - au}$

Properties of Soham transform

i) Linearity Property

$$S\{af(t) + bg(t)\} = aS\{f(t)\} + bS\{g(t)\}$$

ii) Scaling Property

$$S\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

Soham transform of Derivatives

$$i) S\{f'(t)\} = \frac{1}{u} F(u) - f(0)$$

$$ii) S\{f''(t)\} = \frac{1}{u^2} F(u) - \frac{f(0)}{u} - f'(0)$$

28. Anuj Transform[7]

The Anuj transform is defined by

$$A\{f(t)\} = u \int_0^{\infty} f(t) e^{-ut} dt$$

Anuj transform of some elementary functions are

Function	Anuj transform
1	1
t	$\frac{1}{u}$
t <sup>n</sup>	$\frac{n!}{u^n}$
e <sup>at</sup>	$\frac{u}{u-a}$

Properties of Anuj Transform

1) Linearity Property

$$A\{af(t) + bg(t)\} = aA\{f(t)\} + bA\{g(t)\}$$

2) Exponential Shift Property

$$A\{e^{at}f(t)\} = F(u-a)$$

Anuj Transform of Derivatives

$$i) A\{f'(t)\} = uF(u) - uf(0)$$

$$ii) A\{f''(t)\} = u^2F(u) - u^2f(0) - uf'(0)$$

29. Emad Sara Transform[40]

The Emad Sara transform is defined as

$$E\{f(t)\} = \frac{1}{u} \int_0^{\infty} f(t) e^{-ut} dt$$

Emad Sara transform of some elementary functions

are

Function	Emad Sara transform
1	$\frac{1}{u^2}$
t	$\frac{1}{u^3}$
t <sup>n</sup>	$\frac{n!}{u^{n+2}}$
e <sup>at</sup>	$\frac{1}{u(u-a)}$

Properties of Emad Sara transform

i) Linearity Property

$$E\{af(t) + bg(t)\} = aE\{f(t)\} + bE\{g(t)\}$$

(ii) Scaling Property

$$E\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

Emad Sara transform of Derivatives

$$i) E\{f'(t)\} = uF(u) - \frac{f(0)}{u}$$

$$ii) E\{f''(t)\} = u^2F(u) - f(0) - \frac{f'(0)}{u}$$

30. Emad Falih Transform[29]

The Emad Falih transform is defined by

$$E\{f(t)\} = u^2 \int_0^{\infty} f(t) e^{-t/u} dt$$

Emad Falih transform of some elementary functions are

Function	Emad Falih transform
1	u <sup>3</sup>
t	u <sup>4</sup>
t <sup>n</sup>	n! u <sup>n+3</sup>
e <sup>at</sup>	$\frac{u^3}{1-au}$

Properties of Emad Sara transform

1) Linearity Property

$$E\{af(t) + bg(t)\} = aE\{f(t)\} + bE\{g(t)\}$$

2) Exponential Shift Property

$$E\{e^{at}f(t)\} = F\left(\frac{u}{1-au}\right)$$

Emad Falih transform of Derivatives

$$i) E\{f'(t)\} = \frac{1}{u} F(u) - u^2f(0)$$

$$ii) E\{f''(t)\} = \frac{1}{u^2} F(u) - uf(0) - u^2f'(0)$$

31. General Integral Transform by Jafari[23]

The general integral transform introduced by Hassan Jafari is defined by

$$J\{f(t)\} = \int_a^b K(s, t) f(t) dt$$

where K(s, t) is the kernel of the transform.

general integral transform of some elementary functions are

Function	General integral transform
1	$\frac{u}{s}$

t	$\frac{u^2}{s^2}$
t <sup>n</sup>	$\frac{n! u^{n+1}}{s^{n+1}}$

Properties of Emad Sara transform

1) Linearity Property

$$J\{af(t) + bg(t)\} = aJ\{f(t)\} + bJ\{g(t)\}$$

2) Convolution Property

$$J\{f * g\} = J\{f\} \cdot J\{g\}$$

General integral transform of Derivatives

$$i) J\{f'(t)\} = sF(s) - f(0)$$

32. AR Transform[74]

The AR transform is defined as

$$AR\{f(t)\} = \int_0^\infty f(t) e^{-st/u} dt$$

AR transform of some elementary functions are

Function	AR transform
1	$\frac{u}{s}$
t	$\frac{u^2}{s^2}$
t <sup>n</sup>	$\frac{n! u^{n+1}}{s^{n+1}}$

Properties of Emad AR transform

1) Linearity Property

$$AR\{af(t) + bg(t)\} = aAR\{f(t)\} + bAR\{g(t)\}$$

2) Scaling Property

$$AR\{f(at)\} = \frac{1}{a} F\left(\frac{s}{au}\right)$$

AR transform of Derivatives

$$i) AR\{f'(t)\} = \frac{s}{u} F(s, u) - f(0)$$

$$ii) AR\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - \frac{s}{u} f(0) - f'(0)$$

33. Complex SEE Transform[44]

The Complex SEE transform is defined by

$$C\{f(t)\} = \int_0^\infty f(t) e^{-i\omega t} dt$$

where  $i = \sqrt{-1}$ .

Complex SEE transform of some elementary functions are

Function	Complex SEE transform
1	$\frac{1}{i\omega}$
e <sup>at</sup>	$\frac{1}{i\omega - a}$
sin at	$\frac{a}{\omega^2 - a^2}$
cos at	$\frac{i\omega}{\omega^2 - a^2}$

Function	Complex SEE transform
1	$\frac{1}{i\omega}$
e <sup>at</sup>	$\frac{1}{i\omega - a}$
sin at	$\frac{a}{\omega^2 - a^2}$
cos at	$\frac{i\omega}{\omega^2 - a^2}$

Properties of Complex SEE transform

i) Linearity Property

$$C\{af(t) + bg(t)\} = aC\{f(t)\} + bC\{g(t)\}$$

(ii) Frequency Shift Property

$$C\{e^{iat}f(t)\} = F(\omega - a)$$

Complex SEE transform of Derivatives

$$i) C\{f'(t)\} = i\omega F(\omega) - f(0)$$

$$ii) C\{f''(t)\} = (i\omega)^2 F(\omega) - i\omega f(0) - f'(0)$$

34. SEA transform[75]

The SEA transform of a function f(t) is defined as

$$SEA\{f(t)\} = \frac{1}{u^2} \int_0^\infty f(t) e^{-t/u} dt$$

SEA transform of some elementary functions are

Function	SEA transform
1	$\frac{1}{u}$
t	$\frac{1}{u^2}$
t <sup>n</sup>	$\frac{n!}{u^{n+1}}$
e <sup>at</sup>	$\frac{1}{u(1-au)}$

(i) Linearity Property

$$SEA\{af(t) + bg(t)\} = aSEA\{f(t)\} + bSEA\{g(t)\}$$

(ii) Scaling Property

$$SEA\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

SEA transform of Derivatives

$$i) SEA\{f'(t)\} = \frac{1}{u} F(u) - \frac{f(0)}{u^2}$$

$$ii) SEA\{f''(t)\} = \frac{1}{u^2} F(u) - \frac{f(0)}{u^3} - \frac{f'(0)}{u^2}$$

35. GF1 Integral Transform[59]

The GF1 integral transform is defined by

$$GF1\{f(t)\} = u \int_0^\infty f(t) e^{-ut} dt$$

GF1 integral transform of some elementary functions are

Function	GF1 integral transform
1	$\frac{1}{u}$
t	$\frac{1}{u^2}$

$t^n$	$\frac{n!}{u^n}$
$e^{at}$	$\frac{u}{u-a}$

(i) Linearity Property

$$GF1\{af(t) + bg(t)\} = aGF1\{f(t)\} + bGF1\{g(t)\}$$

(ii) Exponential Shift Property

$$GF1\{e^{at}f(t)\} = F(u-a)$$

GF1 integral transform of Derivatives

i)  $GF1\{f'(t)\} = uF(u) - uf(0)$

ii)  $GF1\{f''(t)\} = u^2F(u) - u^2f(0) - uf'(0)$

36.KKAT Transform[28]

The KKAT transform is defined as

$$K\{f(t)\} = u \int_0^\infty f(t) e^{-st/u} dt$$

KKAT transform of some elementary functions are

Function	KKAT transform
1	$\frac{u^2}{s}$
t	$\frac{u^3}{s^2}$
$t^n$	$\frac{n! u^{n+2}}{s^{n+1}}$
$e^{at}$	$\frac{u^2}{s-au}$

i) Linearity Property

$$K\{af(t) + bg(t)\} = aK\{f(t)\} + bK\{g(t)\}$$

ii) Scaling Property

$$K\{f(at)\} = \frac{1}{a} F\left(\frac{s}{au}\right)$$

KKAT transform of Derivatives

i)  $K\{f'(t)\} = \frac{s}{u} F(s, u) - uf(0)$

ii)  $K\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - sf(0) - uf'(0)$

37.Mellin Transform[35]

Definition

The Mellin transform of  $f(t)$  is defined by

$$M\{f(t)\} = \int_0^\infty t^{s-1} f(t) dt$$

Mellin transform of some elementary functions are

Function	Mellin transform
$e^{-t}$	$\Gamma(s)$
$t^n e^{-t}$	$\Gamma(n+s)$
$\sin t$	$\Gamma(s) \operatorname{sinfracpi}2$

(i) Linearity Property

$$M\{af(t) + bg(t)\} = aM\{f(t)\} + bM\{g(t)\}$$

(ii) Scaling Property

$$M\{f(at)\} = a^{-s} F(s)$$

Mellin transform of Derivatives

i)  $M\{f'(t)\} = -(s-1)F(s-1)$

ii)  $M\{f''(t)\} = (s-1)(s-2)F(s-2)$

38.RAHMOH Transform[17]

The RAHMOH transform is defined as

$$R\{f(t)\} = \int_0^\infty f(t) e^{-t/u} dt$$

RAHMOH transform of some elementary functions

are

Function	RAHMOH transform
1	u
t	$u^2$
$t^n$	$n! u^{n+1}$
$e^{at}$	$\frac{u}{1-au}$

1) Linearity Property

$$R\{af(t) + bg(t)\} = aR\{f(t)\} + bR\{g(t)\}$$

2) Exponential Shift Property

$$R\{e^{at}f(t)\} = F\left(\frac{u}{1-au}\right)$$

RAHMOH transform of Derivatives

i)  $R\{f'(t)\} = \frac{1}{u} F(u) - f(0)$

ii)  $R\{f''(t)\} = \frac{1}{u^2} F(u) - \frac{f(0)}{u} - f'(0)$

39.HK Transform[22]

The HK transform is defined by

$$HK\{f(t)\} = u^2 \int_0^\infty f(t) e^{-ut} dt$$

HK transform of some elementary functions are

Function	HK transform
1	u
t	1
$t^n$	$\frac{n!}{u^{n-1}}$
$e^{at}$	$\frac{u^2}{u-a}$

1) Linearity Property

$$HK\{af(t) + bg(t)\} = aHK\{f(t)\} + bHK\{g(t)\}$$

(ii) Scaling Property

$$HK\{f(at)\} = \frac{1}{a^2} F\left(\frac{u}{a}\right)$$

HK transform of Derivatives

- i)  $HK\{f'(t)\} = uF(u) - u^2f(0)$
- ii)  $HK\{f''(t)\} = u^2F(u) - u^3f(0) - u^2f'(0)$

40.Khalouta Transform[32]

The Khalouta transform is defined as

$$K\{f(t)\} = \frac{1}{u} \int_0^\infty f(t) e^{-st/u} dt$$

Khalouta transform of some elementary functions are

Function	Khalouta transform
1	$\frac{1}{s}$
t	$\frac{u}{s^2}$
t <sup>n</sup>	$\frac{n! u^n}{s^{n+1}}$
e <sup>at</sup>	$\frac{1}{s - au}$

1) Linearity Property

$$K\{af(t) + bg(t)\} = aK\{f(t)\} + bK\{g(t)\}$$

2) Exponential Shift Property

$$K\{e^{at}f(t)\} = F(s - au)$$

Khalouta transform of Derivatives

- i)  $K\{f'(t)\} = \frac{s}{u} F(s, u) - \frac{f(0)}{u}$
- ii)  $K\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - \frac{s}{u^2} f(0) - \frac{f'(0)}{u}$

41.Hunaiber Transform[4]

The Hunaiber transform is defined by

$$H\{f(t)\} = \int_0^\infty f(t) e^{-ut} dt$$

Hunaiber transform of some elementary functions are

Function	Hunaiber transform
1	$\frac{1}{u}$
t	$\frac{1}{u^2}$
t <sup>n</sup>	$\frac{n!}{u^{n+1}}$
e <sup>at</sup>	$\frac{1}{u - a}$

i) Linearity Property

$$H\{af(t) + bg(t)\} = aH\{f(t)\} + bH\{g(t)\}$$

ii) Scaling Property

$$H\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

Hunaiber transform of Derivatives:

- i)  $H\{f'(t)\} = uF(u) - f(0)$
- ii)  $H\{f''(t)\} = u^2F(u) - uf(0) - f'(0)$

42.Abaub Shkheam Transform[25]

The Abaub Shkheam transform is defined as

$$A\{f(t)\} = \int_0^\infty e^{-st/u} f(t) dt$$

Abaub Shkheam transform of some elementary functions are

Function	Abaub Shkheam transform
1	$\frac{u}{s}$
t	$\frac{u^2}{s^2}$
t <sup>n</sup>	$\frac{n! u^{n+1}}{s^{n+1}}$

i) Linearity Property

$$A\{af(t) + bg(t)\} = aA\{f(t)\} + bA\{g(t)\}$$

Abaub Shkheam transform of Derivatives

$$i) A\{f'(t)\} = \frac{s}{u} F(s, u) - f(0)$$

43.AMJ Transform[22]

The AMJ transform is defined by

$$AMJ\{f(t)\} = \int_0^\infty f(t) e^{-st} dt$$

AMJ transform of some elementary functions are

Function	AMJ transform
1	$\frac{1}{s}$
t	$\frac{1}{s^2}$
t <sup>n</sup>	$\frac{n!}{s^{n+1}}$
e <sup>at</sup>	$\frac{1}{s - a}$

1) Linearity Property

$$AMJ\{af(t) + bg(t)\} = aAMJ\{f(t)\} + bAMJ\{g(t)\}$$

2) Shifting Property

$$AMJ\{e^{at}f(t)\} = F(s - a)$$

AMJ transform of Derivatives

- i)  $AMJ\{f'(t)\} = sF(s) - f(0)$
- ii)  $AMJ\{f''(t)\} = s^2F(s) - sf(0) - f'(0)$

44.g-Transform[13]

The g-transform is defined as

$$g\{f(t)\} = \frac{1}{u^2} \int_0^{\infty} f(t) e^{-ut} dt$$

g-transform of some elementary functions are

Function	g-transform
1	$\frac{1}{u^3}$
t	$\frac{1}{u^4}$
t <sup>n</sup>	$\frac{n!}{u^{n+3}}$
e <sup>at</sup>	$\frac{1}{u^2(u-a)}$

1) Linearity Property

$$g\{af(t) + bg(t)\} = ag\{f(t)\} + bg\{g(t)\}$$

2) Scaling Property

$$g\{f(at)\} = \frac{1}{a^2} F\left(\frac{u}{a}\right)$$

g-transform of Derivatives

i)  $g\{f'(t)\} = uF(u) - \frac{f(0)}{u^2}$

ii)  $g\{f''(t)\} = u^2F(u) - \frac{f(0)}{u} - \frac{f'(0)}{u^2}$

45.Quideen Transformation[22]

The Quideen transformation of a function f(t) is defined by

$$O\{f(t)\} = \int_0^{\infty} f(t) e^{-t/u} dt$$

Quideen transform of some elementary functions are

Function	Quideen transformation
1	u
t	u <sup>2</sup>
t <sup>n</sup>	n! u <sup>n+1</sup>
e <sup>at</sup>	$\frac{u}{1-au}$

1) Linearity Property

$$O\{af(t) + bg(t)\} = aO\{f(t)\} + bO\{g(t)\}$$

2) Scaling Property

$$O\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

3) Exponential Shift Property

$$O\{e^{at}f(t)\} = F\left(\frac{u}{1-au}\right)$$

Quideen transformation of Derivatives

i)  $O\{f'(t)\} = \frac{1}{u} F(u) - f(0)$

ii)  $O\{f''(t)\} = \frac{1}{u^2} F(u) - \frac{f(0)}{u} - f'(0)$

46.Fareeha Transform[53]

The Fareeha transform is defined as

$$F\{f(t)\} = \int_0^{\infty} e^{-st} f(t) dt$$

Fareeha transform of some elementary functions are

Function	Fareeha transform
1	$\frac{1}{s}$
t	$\frac{1}{s^2}$
t <sup>n</sup>	$\frac{n!}{s^{n+1}}$
e <sup>at</sup>	$\frac{u}{1-au}$
sin at	$\frac{a}{s^2 + a^2}$
cos at	$\frac{s}{s^2 + a^2}$

(i) Linearity Property

$$F\{af(t) + bg(t)\} = aF\{f(t)\} + bF\{g(t)\}$$

(ii) Frequency Shift Property

$$F\{e^{at}f(t)\} = F(s-a)$$

(iii) Differentiation Property

$$F\{tf(t)\} = -\frac{d}{ds} F(s)$$

Fareeha transform of Derivatives

i)  $F\{f'(t)\} = sF(s) - f(0)$

ii)  $F\{f''(t)\} = s^2F(s) - sf(0) - f'(0)$

47.Abdallah Group Transform[20]

The Abdallah Group transform is defined by

$$A\{f(t)\} = \int_0^{\infty} K(s,t)f(t) dt$$

where K(s, t) is the kernel function.

(i) Linearity Property

$$A\{af(t) + bg(t)\} = aA\{f(t)\} + bA\{g(t)\}$$

(ii) Convolution Property

$$A\{f * g\} = A\{f\} \cdot A\{g\}$$

Abdallah Group transform of Derivatives

i)  $A\{f'(t)\} = sF(s) - f(0)$

ii)  $A\{f''(t)\} = s^2F(s) - sf(0) - f'(0)$

48.Rangaig Transform[46]

The Rangaig transform of a function f(t) is defined as

$$R\{f(t)\} = \int_0^{\infty} f(t) e^{-st/u} dt$$

Rangaig transform of some elementary functions are

Function	Rangaig transform
1	$\frac{u}{s}$
t	$\frac{u^2}{s^2}$
t <sup>n</sup>	$\frac{n! u^{n+1}}{s^{n+1}}$
e <sup>at</sup>	$\frac{u}{s - au}$

(i) Linearity Property

$$R\{af(t) + bg(t)\} = aR\{f(t)\} + bR\{g(t)\}$$

(ii) Scaling Property

$$R\{f(at)\} = \frac{1}{a} F\left(\frac{s}{au}\right)$$

(iii) Exponential Shift Property

$$R\{e^{at}f(t)\} = F(s - au)$$

Rangaig transform of Derivatives

$$i)R\{f'(t)\} = \frac{s}{u} F(s, u) - f(0)$$

$$ii)R\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - \frac{s}{u} f(0) - f'(0)$$

49.Emad-Salam-Elaf Transform[63]

The Emad-Salam-Elaf transform is defined by

$$E\{f(t)\} = \frac{1}{u} \int_0^\infty e^{-st/u} f(t) dt$$

Emad-Salam-Elaf transform of some elementary functions are

Function	Emad-Salam-Elaf
1	$\frac{1}{s}$
t	$\frac{u}{s^2}$
t <sup>n</sup>	$\frac{n! u^n}{s^{n+1}}$
e <sup>at</sup>	$\frac{1}{s - au}$
sin at	$\frac{au}{s^2 + a^2u^2}$
cos at	$\frac{s}{s^2 + a^2u^2}$

(i) Linearity Property

$$E\{af(t) + bg(t)\} = aE\{f(t)\} + bE\{g(t)\}$$

(ii) Exponential Shift Property

$$E\{e^{at}f(t)\} = F(s - au)$$

(iii) Scaling Property

$$E\{f(at)\} = \frac{1}{a} F\left(\frac{s}{au}\right)$$

Emad-Salam-Elaf transform of Derivatives

$$i)E\{f'(t)\} = \frac{s}{u} F(s, u) - \frac{f(0)}{u}$$

$$ii)E\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - \frac{s}{u^2} f(0) - \frac{f'(0)}{u}$$

50.Upadhya Transform[54]

The Upadhya transform of a function f(t) is defined by

$$U\{f(t)\} = \frac{1}{u} \int_0^\infty f(t) e^{-t/u} dt$$

Upadhya transform of some elementary functions are

Function	Upadhya Transform
1	1
t	u
t <sup>n</sup>	n! u <sup>n</sup>
e <sup>at</sup>	$\frac{1}{1 - au}$
sin at	$\frac{au}{1 + a^2u^2}$
cos at	$\frac{1}{1 + a^2u^2}$

1) Linearity Property

$$U\{af(t) + bg(t)\} = aU\{f(t)\} + bU\{g(t)\}$$

2) Scaling Property

$$U\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

3) Exponential Shift Property

$$U\{e^{at}f(t)\} = F\left(\frac{u}{1 - au}\right)$$

Upadhya transform of Derivatives

$$i)U\{f'(t)\} = \frac{1}{u} F(u) - \frac{f(0)}{u}$$

$$ii)U\{f''(t)\} = \frac{1}{u^2} F(u) - \frac{f(0)}{u^2} - \frac{f'(0)}{u}$$

51.Laplace Transform[58]

The Laplace Transform of a function f(t) is defined by

$$L\{f(t)\} = \int_0^\infty e^{-st} f(t) dt$$

Laplace Transform of some elementary functions are

Function	Laplace Transform
1	$\frac{1}{s}$
t	$\frac{1}{s^2}$
t <sup>n</sup>	$\frac{n!}{s^{n+1}}$

$e^{at}$	$\frac{1}{s-a}$
$\sin at$	$\frac{a}{s^2+a^2}$
$\cos at$	$\frac{s}{s^2+a^2}$

1) Linearity

$$L\{af(t) + bg(t)\} = aL\{f(t)\} + bL\{g(t)\}$$

2) First Shifting Property

$$L\{e^{at}f(t)\} = F(s-a)$$

3) Change of Scale

$$L\{f(at)\} = \frac{1}{a}F\left(\frac{s}{a}\right)$$

i)  $L\{f'(t)\} = sF(s) - f(0)$

ii)  $L\{f''(t)\} = s^2F(s) - sf(0) - f'(0)$

52. Sumudu Transform[24]

$$S\{f(t)\} = \int_0^\infty f(ut) e^{-t} dt$$

Sumudu Transform of some elementary functions are

Function	Sumudu Transform
1	1
t	u
$t^n$	$n! u^n$
$e^{at}$	$\frac{1}{1-au}$
$\sin at$	$\frac{au}{1+a^2u^2}$
$\cos at$	$\frac{1}{1+a^2u^2}$

1) Linearity

$$S\{af(t) + bg(t)\} = aS\{f(t)\} + bS\{g(t)\}$$

2) Scaling Property

$$S\{f(at)\} = F(au)$$

3) Differentiation Property

$$S\{tf(t)\} = u \frac{d}{du} F(u)$$

Sumudu Transform of Derivatives

i)  $S\{f'(t)\} = \frac{F(u)-f(0)}{u}$

ii)  $S\{f''(t)\} = \frac{F(u)-f(0)-uf'(0)}{u^2}$

53. Laplace-Carson Transform[58]

$$LC\{f(t)\} = s \int_0^\infty e^{-st} f(t) dt$$

Laplace-Carson Transform of some elementary functions are

Function	Laplace-Carson Transform
1	1
t	$\frac{1}{s}$
$t^n$	$\frac{n!}{s^{n+1}}$
$e^{at}$	$\frac{s}{s-a}$
$\sin at$	$\frac{as}{s^2+a^2}$
$\cos at$	$\frac{s^2}{s^2+a^2}$

i) Linearity

$$LC\{af(t) + bg(t)\} = aLC\{f(t)\} + bLC\{g(t)\}$$

ii) Frequency Shift

$$LC\{e^{at}f(t)\} = F(s-a)$$

Laplace-Carson Transform of Derivatives

i)  $LC\{f'(t)\} = sLC\{f(t)\} - sf(0)$

ii)  $LC\{f''(t)\} = s^2LC\{f(t)\} - s^2f(0) - sf'(0)$

54. Natural Transform[28]

$$N\{f(t)\} = \int_0^\infty f(t) e^{-st/ut} dt$$

Laplace-Carson Transform of some elementary functions are

Function	Natural Transform
1	$\frac{u}{s}$
t	$\frac{u^2}{s^2}$
$t^n$	$\frac{n! u^{n+1}}{s^{n+1}}$
$e^{at}$	$\frac{u}{s-au}$
$\sin at$	$\frac{au^2}{s^2+a^2u^2}$
$\cos at$	$\frac{su}{s^2+a^2u^2}$

(i) Linearity

$$N\{af(t) + bg(t)\} = aN\{f(t)\} + bN\{g(t)\}$$

(ii) Exponential Shift

$$N\{e^{at}f(t)\} = F(s-au, u)$$

Natural Transform of Derivatives

i)  $N\{f'(t)\} = \frac{s}{u} F(s, u) - f(0)$

$$\text{ii) } N\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - \frac{s}{u} f(0) - f'(0)$$

55. Elzaki Transform [15]

$$E\{f(t)\} = u \int_0^\infty f(t) e^{-t/u} dt$$

Elzaki Transform of some elementary functions are

Function	Elzaki Transform
1	$u^2$
t	$u^3$
$t^n$	$n! u^{n+2}$
$e^{at}$	$\frac{u^2}{1-au}$
sin at	$\frac{au^3}{1+a^2u^2}$
cos at	$\frac{u^2}{1+a^2u^2}$

i) Linearity

$$E\{af(t) + bg(t)\} = aE\{f(t)\} + bE\{g(t)\}$$

(ii) Scaling Property

$$E\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

Elzaki Transform of Derivatives

$$\text{i) } E\{f'(t)\} = \frac{1}{u} F(u) - uf(0)$$

$$\text{ii) } E\{f''(t)\} = \frac{1}{u^2} F(u) - f(0) - uf'(0)$$

56. Aboodh Transform [1]

$$A\{f(t)\} = \frac{1}{s} \int_0^\infty e^{-st} f(t) dt$$

Aboodh Transform of some elementary functions are

Function	Aboodh Transform
1	$u^2$
t	$u^3$
$t^n$	$n! u^{n+2}$
$e^{at}$	$\frac{u^2}{1-au}$
sin at	$\frac{au^3}{1+a^2u^2}$
cos at	$\frac{u^2}{1+a^2u^2}$

(i) Linearity

$$A\{af(t) + bg(t)\} = aA\{f(t)\} + bA\{g(t)\}$$

(ii) Frequency Shift

$$A\{e^{at}f(t)\} = F(s-a)$$

Aboodh Transform of Derivatives

$$\text{i) } A\{f'(t)\} = sF(s) - \frac{f(0)}{s}$$

$$\text{ii) } A\{f''(t)\} = s^2F(s) - f(0) - \frac{f'(0)}{s}$$

57. ZZ Transform [61]

$$ZZ\{f(t)\} = u \int_0^\infty f(t) e^{-st/u} dt$$

ZZ Transform of some elementary functions are

Function	ZZ Transform
1	$\frac{u^2}{s}$
t	$\frac{u^3}{s^2}$
$t^n$	$\frac{n! u^{n+2}}{s^{n+1}}$
$e^{at}$	$\frac{u^2}{s-au}$
sin at	$\frac{au^3}{s^2+a^2u^2}$
cos at	$\frac{su^2}{s^2+a^2u^2}$

i) Linearity

$$ZZ\{af(t) + bg(t)\} = aZZ\{f(t)\} + bZZ\{g(t)\}$$

(ii) Exponential Shift

$$ZZ\{e^{at}f(t)\} = F(s-au, u)$$

(iii) Scaling Property

$$ZZ\{f(at)\} = \frac{1}{a} F\left(\frac{s}{au}, u\right)$$

ZZ Transform of Derivatives

$$\text{i) } ZZ\{f'(t)\} = \frac{s}{u} F(s, u) - uf(0)$$

$$\text{ii) } ZZ\{f''(t)\} = \frac{s^2}{u^2} F(s, u) - sf(0) - uf'(0)$$

58. Mohand Transform [37]

The Mohand transform of a function  $f(t)$ , defined for  $t \geq 0$ , is given by

$$M\{f(t)\} = u^2 \int_0^\infty f(t) e^{-ut} dt$$

where  $u$  is the transform parameter and the integral converges.

Mohand transform of some elementary functions are

Function	Mohand transform
1	$u$
t	$1$
$t^n$	$\frac{n!}{u^{n-1}}$
$e^{at}$	$\frac{u^2}{u-a}$

1)Linearity

$$M\{af(t) + bg(t)\} = aM\{f(t)\} + bM\{g(t)\}$$

2)Scaling

$$M\{f(at)\} = \frac{1}{a^2} F\left(\frac{u}{a}\right)$$

Mohand transform of Derivatives

i)  $M\{f'(t)\} = uF(u) - u^2f(0)$

59.ZMA Transform[6]

The ZMA Transform of a function f(t), defined for is given by

$$ZMA\{f(t)\} = \frac{1}{u} \int_0^\infty f(t) e^{-st/u} dt$$

ZMA Transform of some elementary functions are

Function	ZMA Transform
1	$\frac{1}{s}$
t	$\frac{u}{s^2}$
t <sup>n</sup>	$\frac{n! u^n}{s^{n+1}}$
e <sup>at</sup>	$\frac{1}{s - au}$

1)Linearity

$$ZMA\{af(t) + bg(t)\} = aZMA\{f(t)\} + bZMA\{g(t)\}$$

2)Scaling Property

$$ZMA\{f(at)\} = \frac{1}{a} F\left(\frac{s}{au}\right)$$

3)Exponential Shift

$$ZMA\{e^{at}f(t)\} = F(s - au, u)$$

ZMA Transform of Derivatives

$$ZMA\{f'(t)\} = \frac{s}{u} F(s, u) - \frac{f(0)}{u}$$

60.NE Transform[60]

The NE Transform of a function f(t), defined for t ≥ 0, is given by

$$NE\{f(t)\} = u \int_0^\infty e^{-\frac{st}{u}} f(t) dt$$

where

s and u are transform parameters,

f(t) is a piecewise continuous function of exponential order

NE Transform of some elementary functions are

Function	NE Transform
1	$\frac{u^2}{s}$

t	$\frac{u^3}{s^2}$
e <sup>at</sup>	$\frac{u^2}{s - au}$
sin (at)	$\frac{au^3}{s^2 + a^2u^2}$

Properties of NE Transform

Let

$$NE\{f(t)\} = F(s, u)$$

1. Linearity Property

If a and b are constants, then

$$NE\{af(t) + bg(t)\} = aNE\{f(t)\} + bNE\{g(t)\}$$

2. Change of Scale Property

For a > 0,

$$NE\{f(at)\} = \frac{1}{a} F\left(\frac{s}{a}, u\right)$$

3. Exponential Shifting Property

If NE{f(t)} = F(s, u), then

$$NE\{e^{at}f(t)\} = F(s - au, u)$$

4. Transform of Multiplication by t

$$NE\{tf(t)\} = -u \frac{\partial F(s, u)}{\partial s}$$

5. Transform of Multiplication by t<sup>n</sup>

$$NE\{t^n f(t)\} = (-u)^n \frac{\partial^n F(s, u)}{\partial s^n}$$

NE Transform of Derivatives

$$NE\{f'(t)\} = \frac{s}{u} F(s, u) - uf(0)$$

61.KAJ Transform[50]

$$KAJ\{f(t)\} = \int_0^\infty f(t) e^{-t/u} dt$$

KAJ Transform of some elementary functions are

Functions	KAJ Transform
1	u
t	u <sup>2</sup>
e <sup>at</sup>	$\frac{u^2}{s - au}$
sin (at)	$\frac{au^3}{s^2 + a^2u^2}$

1)Linearity

2)Scaling

3)Exponential Shift

KAJ Transform of Derivatives

$$KAJ\{f'(t)\} = \frac{1}{u} F(u) - f(0)$$

62. SEJI Transform[64]

$$SEJI\{f(t)\} = \int_0^\infty f(t) e^{-iq(s)t} dt$$

SEJI Transform of some elementary functions are

Function	SEJI Transform
1	$\frac{1}{iq(s)}$
t	$\frac{1}{(u)^2}$
$e^{at}$	$\frac{1}{iq(s) - a}$

- 1) Linearity
- 2) Frequency Shift
- 3) Convolution

SEJI Transform of Derivatives

$$SEJI\{f'(t)\} = iq(s)F(s) - f(0)$$

63. Raj Transform[24]

$$R\{f(t)\} = s \int_0^\infty f(t) e^{-st} dt$$

Raj Transform of some elementary functions are

Function	Raj Transform
1	1
t	$\frac{1}{s}$
$t^n$	$\frac{n!}{s^n}$

Raj Transform of Derivatives

$$R\{f'(t)\} = sR\{f(t)\} - sf(0)$$

64. IMAN Transform[5]

$$IMAN\{f(t)\} = \int_0^\infty f(t) e^{-t/u} dt$$

IMAN Transform of some elementary functions are

Function	IMAN Transform
1	u
t	$u^2$
$e^{at}$	$\frac{u}{1 - au}$

IMAN Transform of Derivatives

$$IMAN\{f'(t)\} = \frac{1}{u} F(u) - f(0)$$

65. INEM Transform[43]

$$INEM\{f(t)\} = \int_0^\infty p(s) e^{-st} f(t) dt$$

- 1) Linearity

- 2) Scaling
- 3) Frequency Shift

INEM Transform of Derivatives

$$INEM\{f'(t)\} = sF(s) - p(s)f(0)$$

66. Rohit Transform[19]

$$R\{f(t)\} = \frac{1}{u} \int_0^\infty f(t) e^{-st/u} dt$$

Rohit Transform of some elementary functions are

Function	Rohit Transform
1	$\frac{1}{s}$
t	$\frac{u}{s^2}$
$e^{at}$	$\frac{1}{s - au}$

Rohit Transform of Derivatives

$$R\{f'(t)\} = \frac{s}{u} F(s, u) - \frac{f(0)}{u}$$

67. DV (Dinesh Verma) Transform[18]

$$DV\{f(t)\} = \frac{1}{u^2} \int_0^\infty f(t) e^{-t/u} dt$$

DV (Dinesh Verma) Transform of some elementary functions are

Function	DV (Dinesh Verma) Transform
1	$\frac{1}{u}$
t	1
$t^n$	$n! u^{n-1}$

DV (Dinesh Verma) Transform of Derivatives

$$G\{f'(t)\} = \frac{s}{u} F(s, u) - \frac{f(0)}{u}$$

68. Gupta Transform[18]

The Gupta Transform of a function  $f(t)$ , defined for  $t \geq 0$ , is given by

$$G\{f(t)\} = \frac{1}{u} \int_0^\infty e^{-\frac{st}{u}} f(t) dt$$

where

s and u are transform variables,

$f(t)$  is piecewise continuous and of exponential order.

- 1. Linearity Property

If a and b are constants, then

$$G\{af(t) + bg(t)\} = aG\{f(t)\} + bG\{g(t)\}$$

Change of Scale Property

For  $a > 0$ ,

$$G\{f(at)\} = \frac{1}{a} F\left(\frac{s}{a}, u\right)$$

Exponential Shifting Property  
If

$$G\{f(t)\} = F(s, u),$$

then

$$G\{e^{at}f(t)\} = F(s - au, u)$$

69. J Transform [43]

The J Transform of a function  $f(t)$ , defined for  $t \geq 0$ , is given by

$$J\{f(t)\} = s \int_0^{\infty} e^{-st} f(t) dt$$

where:

$s$  is the transform parameter,

$f(t)$  is piecewise continuous and of exponential order

1. Linearity Property

If  $a$  and  $b$  are constants, then

$$J\{af(t) + bg(t)\} = aJ\{f(t)\} + bJ\{g(t)\}$$

2. First Shifting Property

$$J\{e^{at}f(t)\} = F(s - a)$$

Function	J Transform
1	1
t	$\frac{1}{s}$
$t^n$	$\frac{n!}{s^{n+1}}$
$e^{at}$	$\frac{1}{s-a}$
$\sin(at)$	$\frac{a}{s^2 + a^2}$
$\cos(at)$	$\frac{s}{s^2 + a^2}$

70. Rishi Transform [31]

The Rishi Transform of a function  $f(t)$ , defined for  $t \geq 0$ , is given by

$$R\{f(t)\} = \frac{1}{u} \int_0^{\infty} e^{-t/u} f(t) dt$$

where  $u$  is the transform parameter and  $f(t)$  is piecewise continuous on  $[0, \infty)$ .

Rishi Transform of some elementary functions are

Function	Rishi Transform
1	1
t	u
$e^{at}$	$\frac{1}{1-au}$
$\sin(at)$	$\frac{1}{1+a^2u^2}$
$\cos(at)$	$\frac{1}{1+a^2u^2}$

1. Linearity Property

If  $a$  and  $b$  are constants, then

$$R\{af(t) + bg(t)\} = aR\{f(t)\} + bR\{g(t)\}$$

2. Change of Scale Property

For  $a > 0$ ,

$$R\{f(at)\} = \frac{1}{a} F\left(\frac{u}{a}\right)$$

3. Exponential Shifting Property

$$R\{e^{at}f(t)\} = F\left(\frac{u}{1-au}\right)$$

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